



Mikro- und Meso-Mechanische Simulationen zum Verformungsverhalten von Tongesteinen

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Content

**1. General comments on
micro-mechanical modelling**

**2. Micro- and meso-mechanical
modelling of Opalinus Clay**



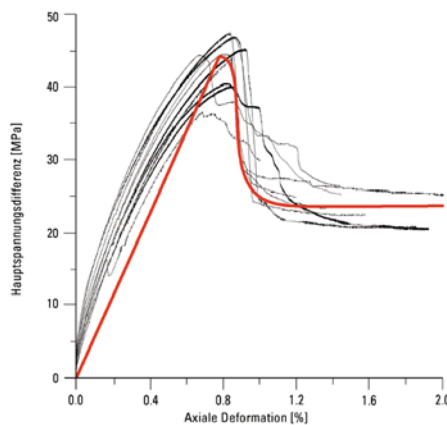
2

Method of approach



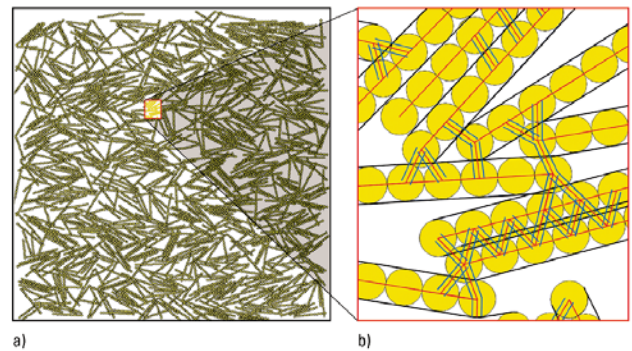
Macro-mechanical view
(scale: dm, m, km)

„Phenomenological“ concept



Micro-mechanical view
(scale: nm, μm , mm)

„Physical“ concept



Micromechanical simulation approaches

Choice of simulation approach

**deformable
polyhedra**



Voronoi-bodies

- more physics, more flexible
- computer-intensiv
- potential of numerical instability

**stiff
spheres**

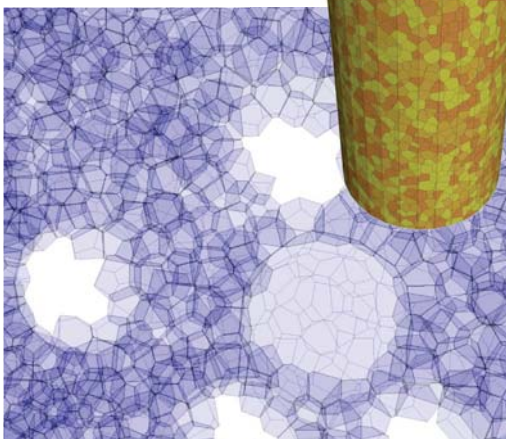
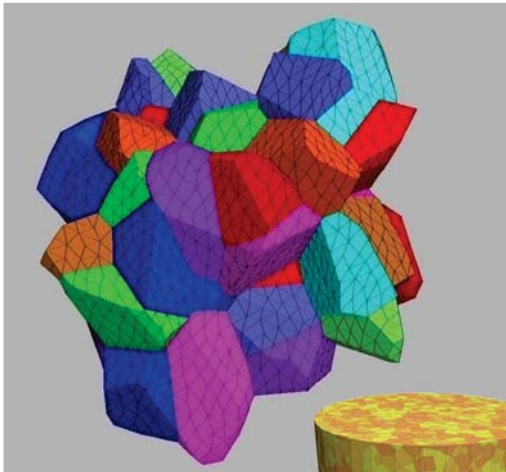


Spheres-Clusters-Clumps

- robust, fast, stable
- physical less flexible

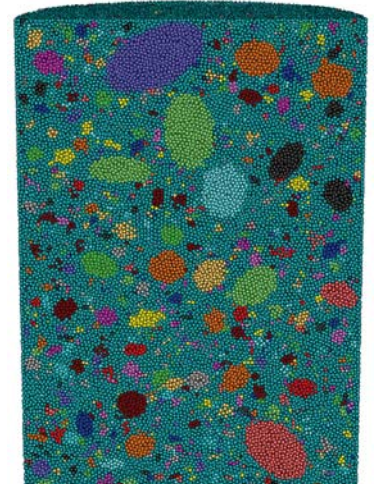
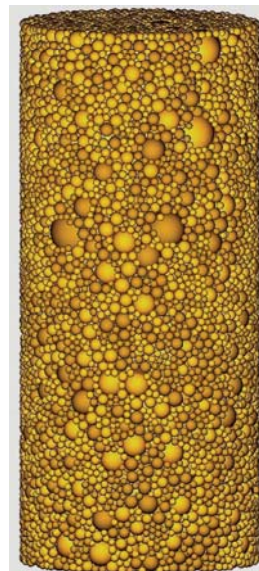
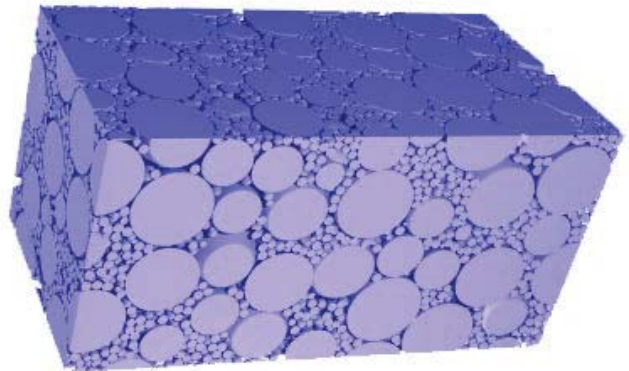
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Generation of models



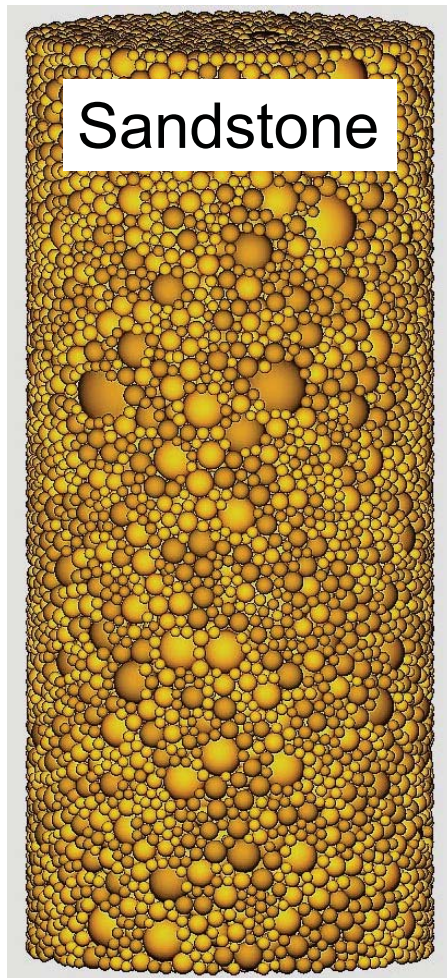
Voronoi Bodies

Spheres – Clumps - Clusters

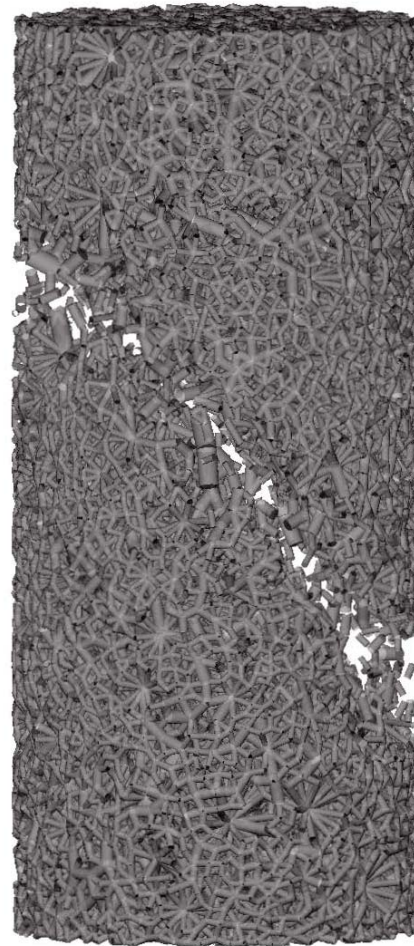


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Model set-up based on spheres according to grain size distribution



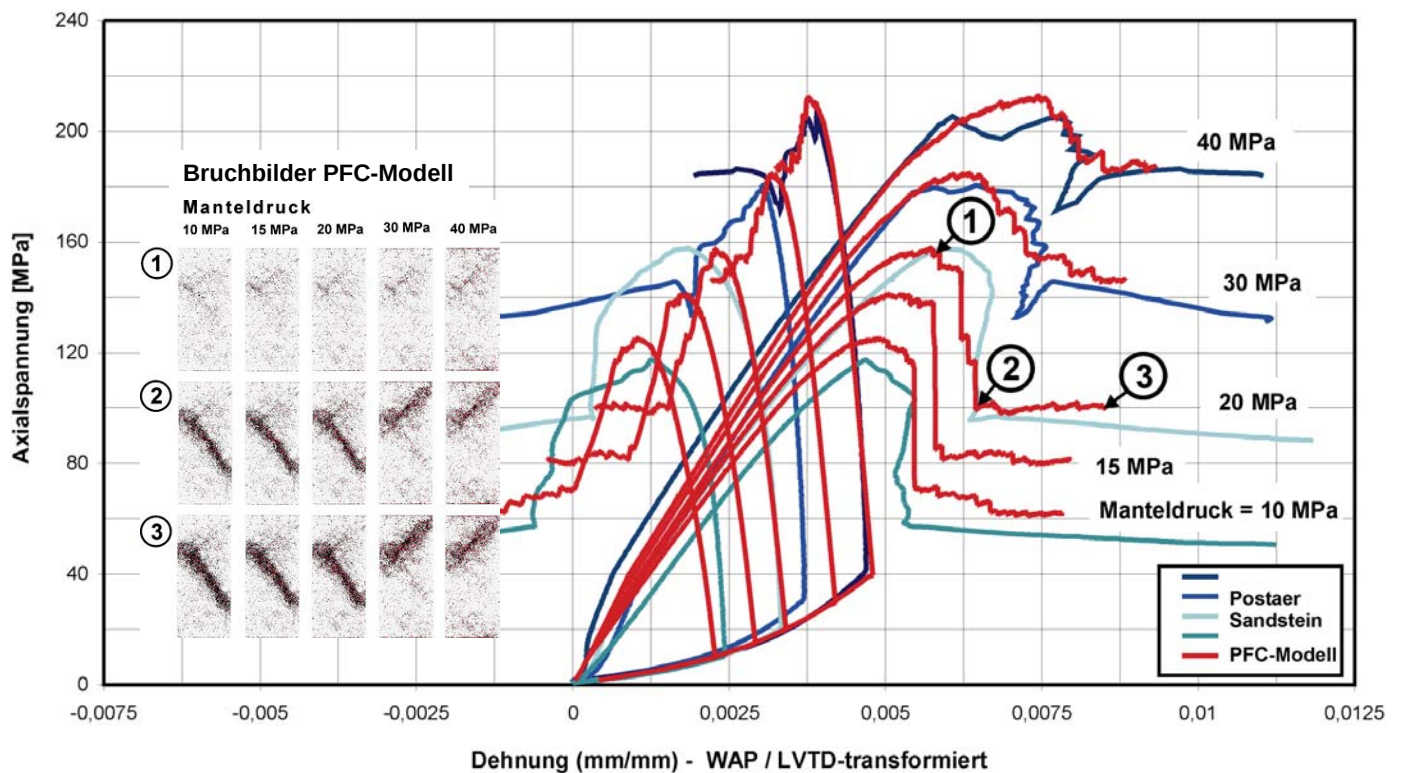
Shear fracture during triaxial testing



Baumgarten & Konietzky 2013

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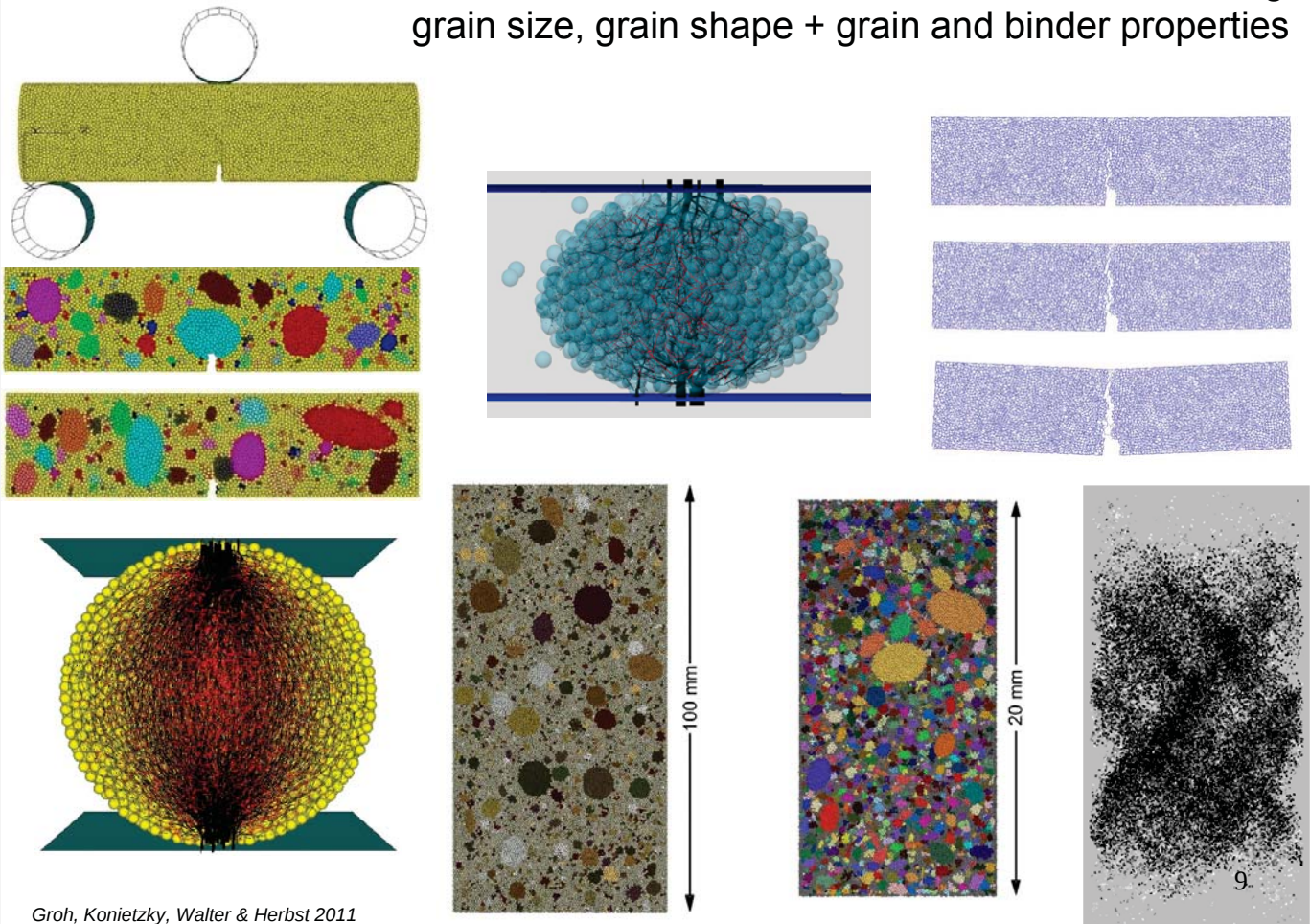
Sandstone



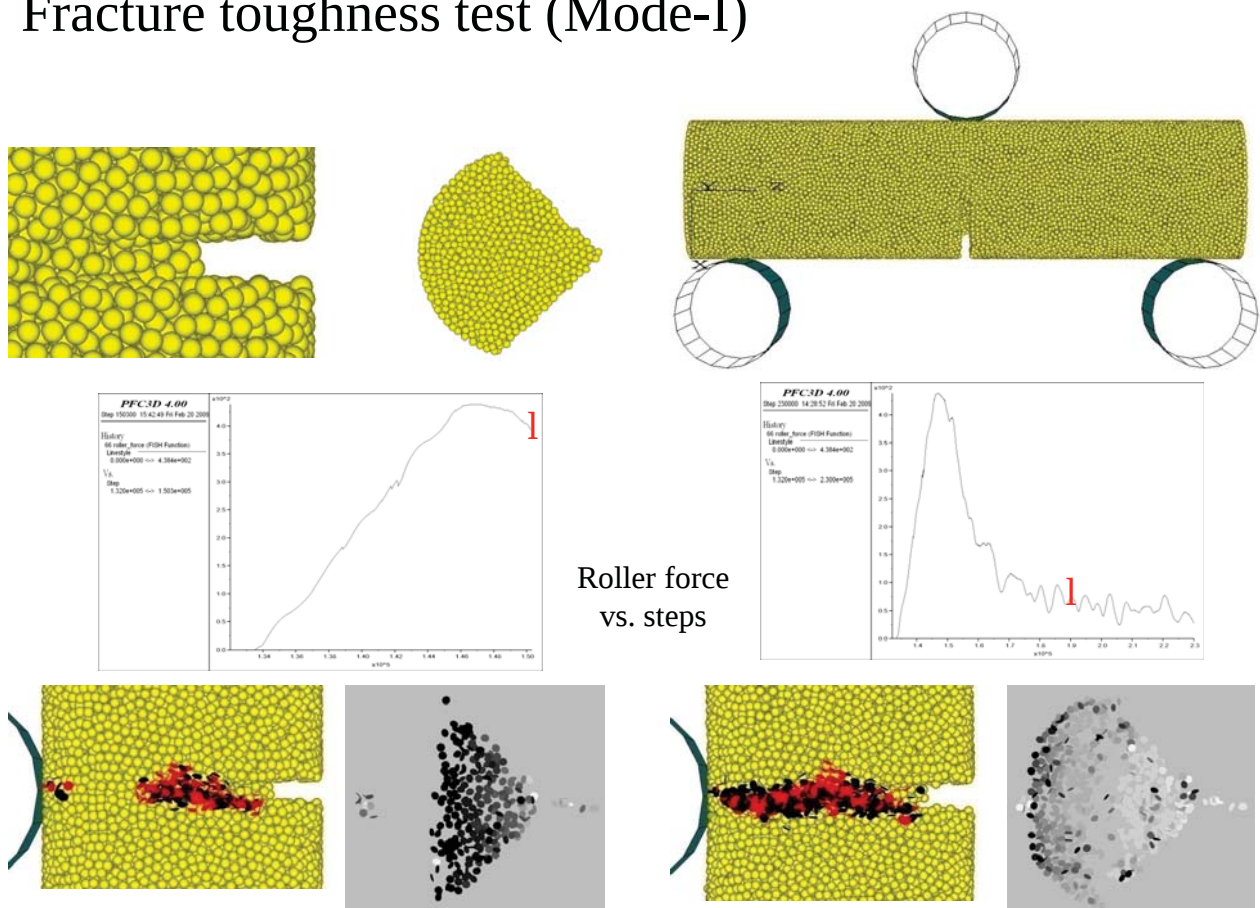
Baumgarten & Konietzky 2013

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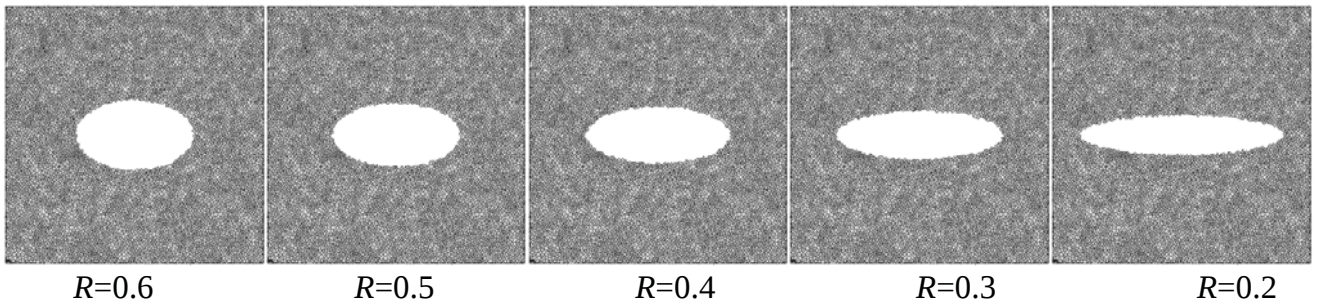
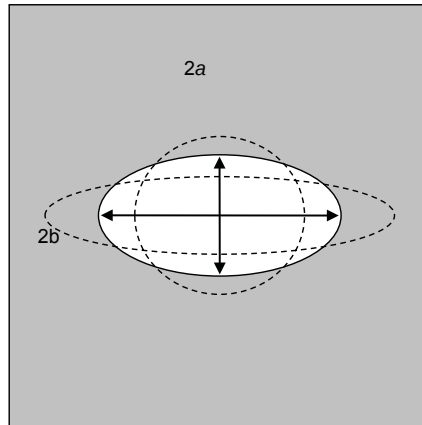
Micromechanical simulation of concrete considering grain size, grain shape + grain and binder properties



Fracture toughness test (Mode-I)



Micro-mechanical model of single pore of different shape

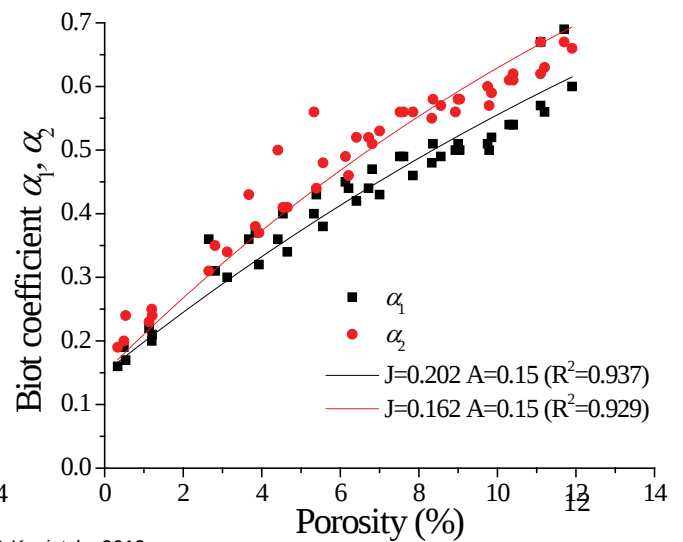
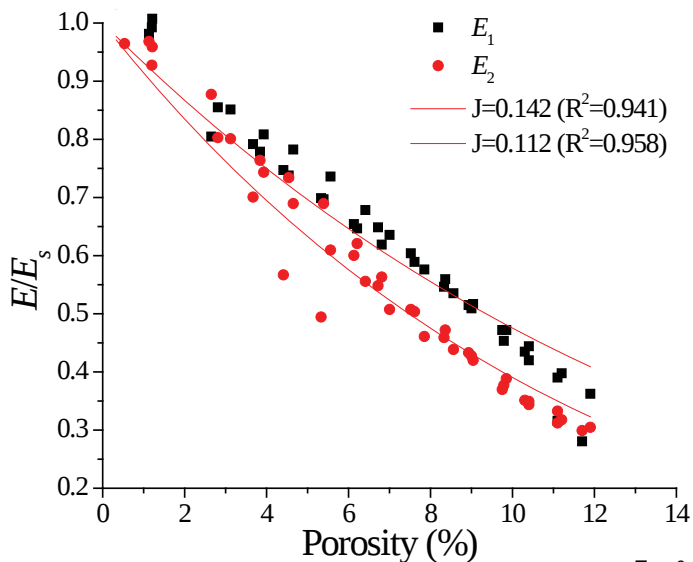
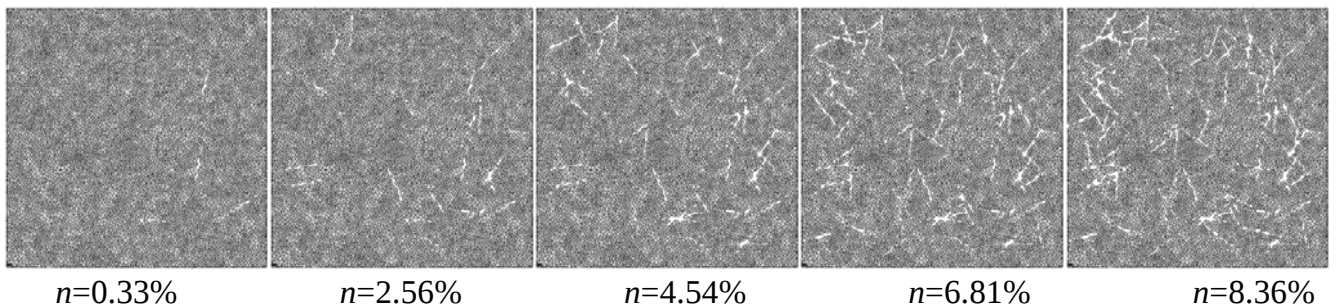


Elliptical pores with different aspect ratio

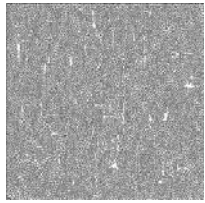
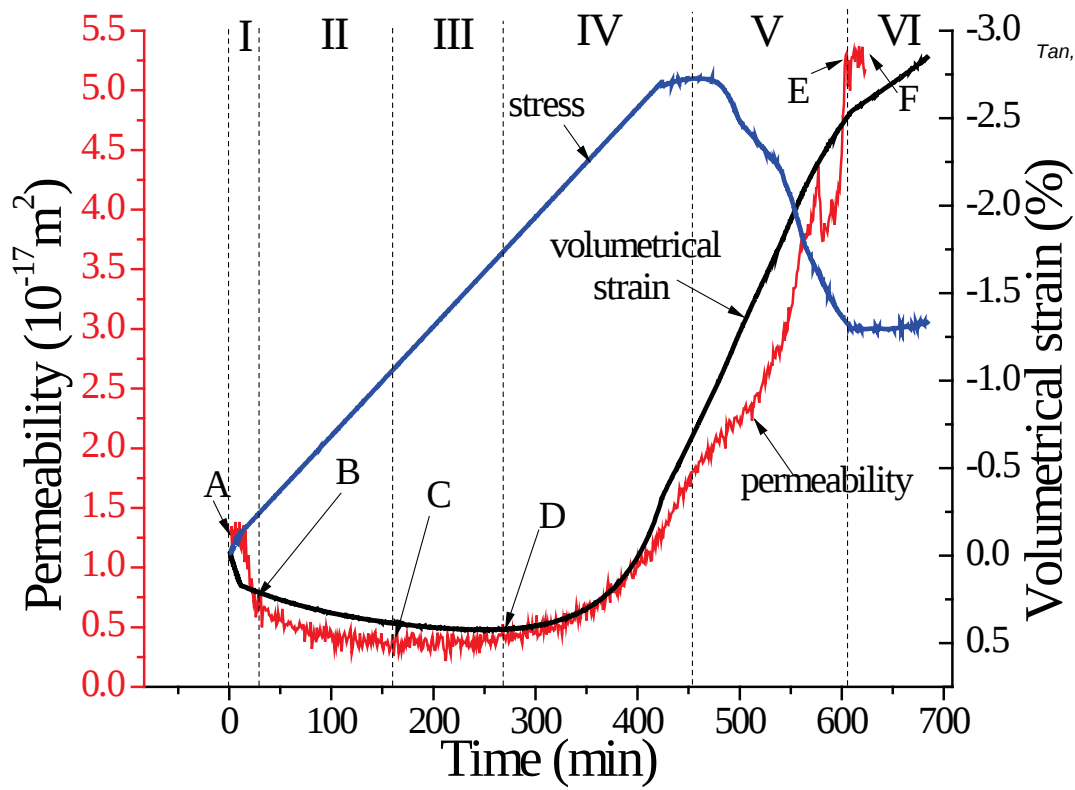
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Tan & Konietzky 2013

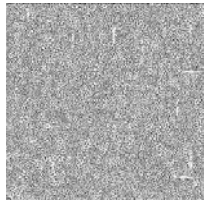
Random elliptical cracks ($S=0.1$)



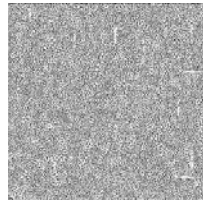
Tan & Konietzky 2013



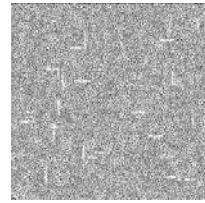
A



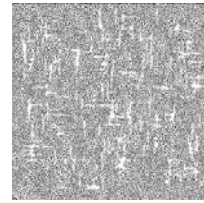
B



C

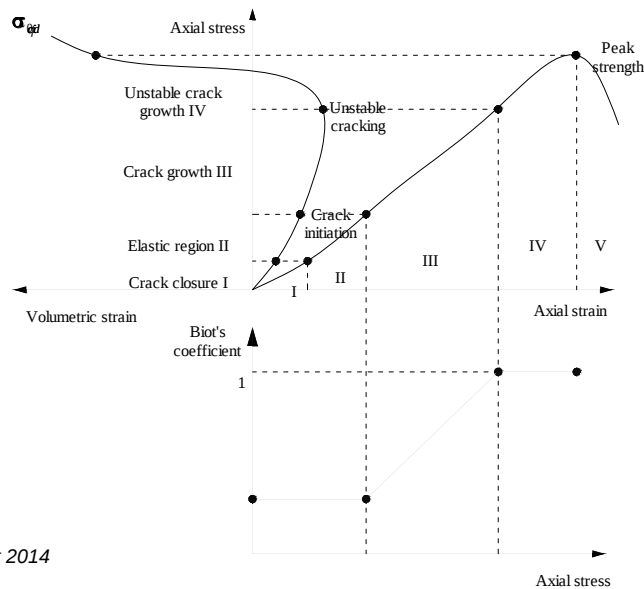
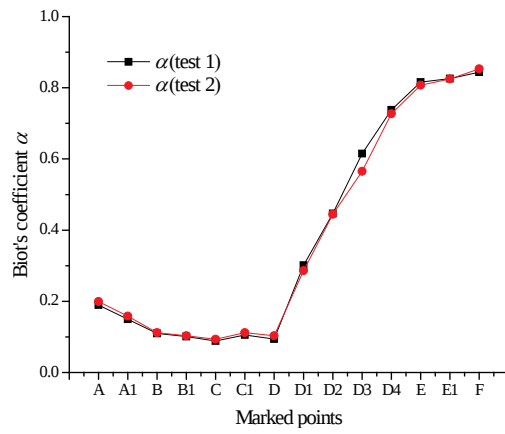
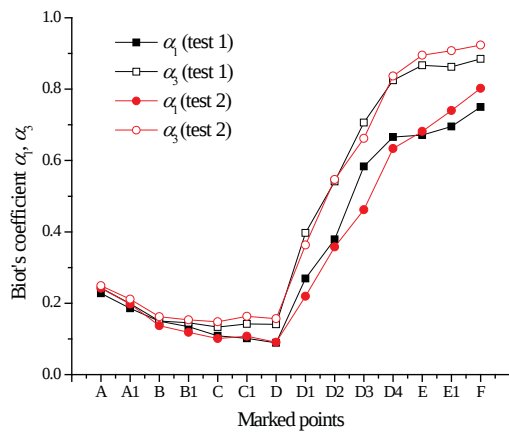


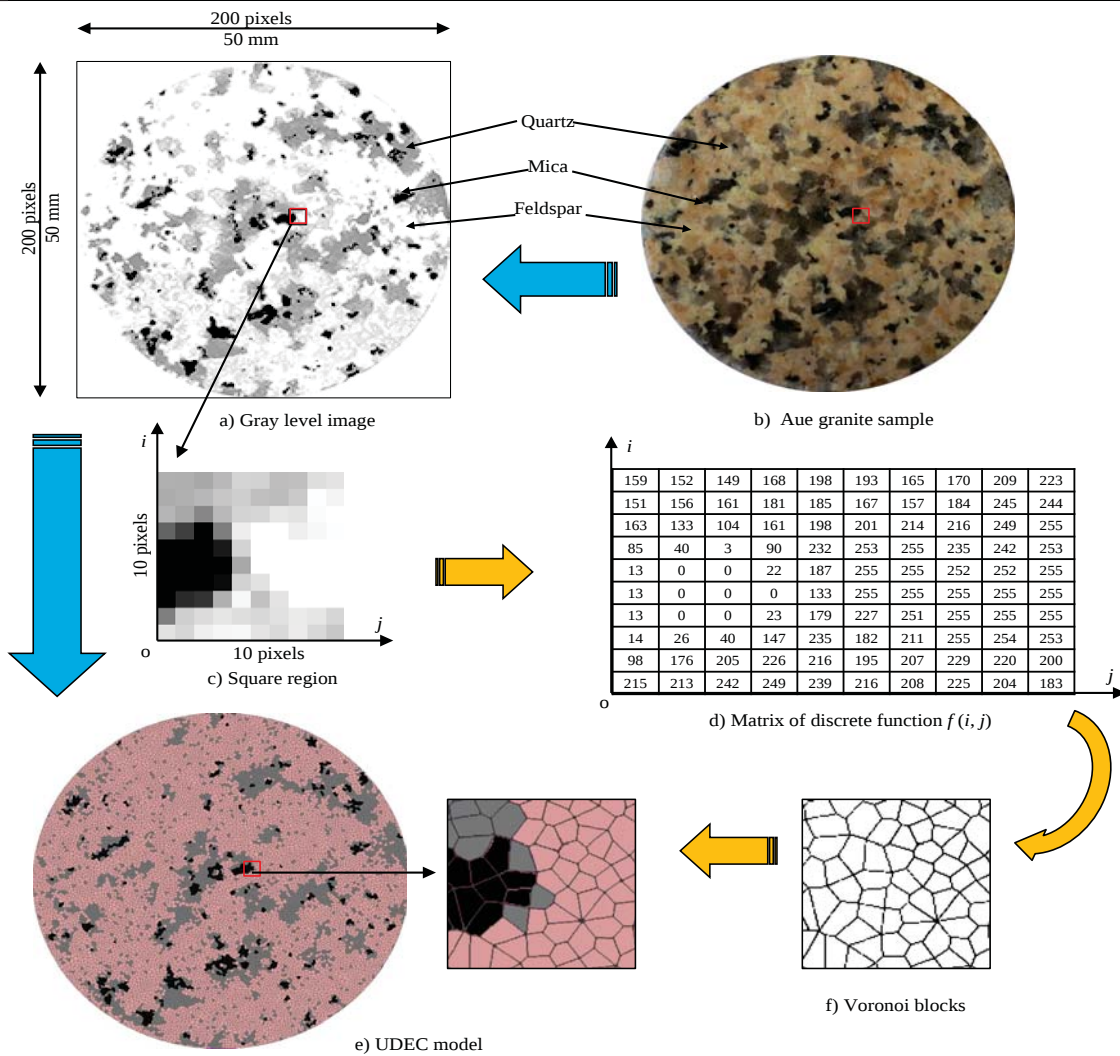
D



E

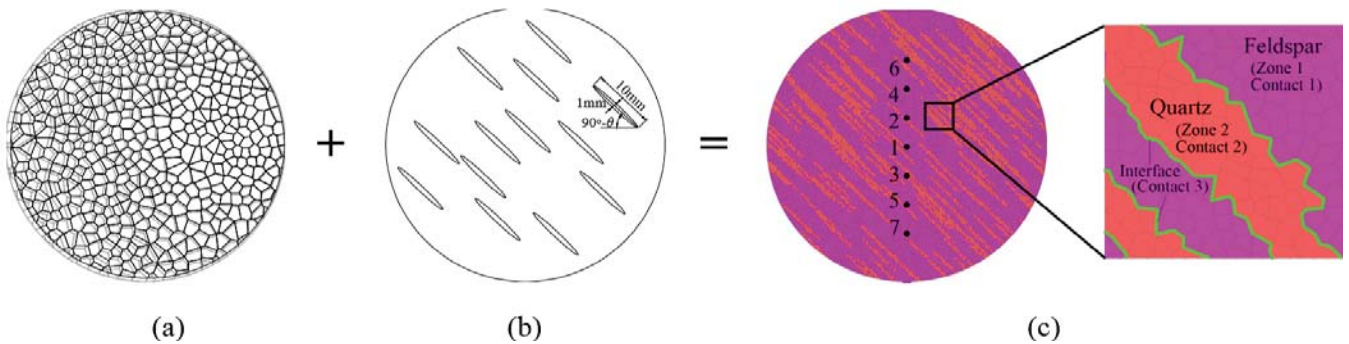
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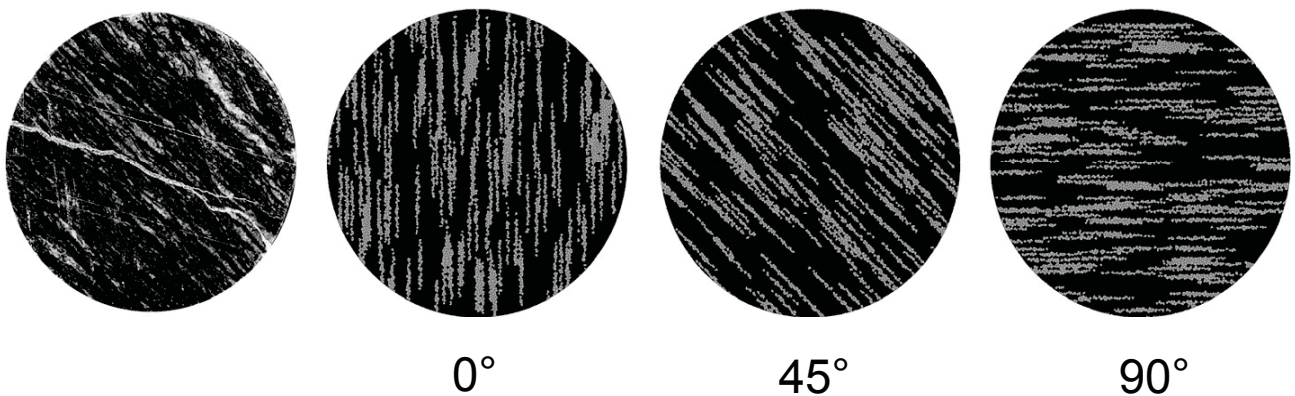


Gray level image technique
to duplicate microstructure

15

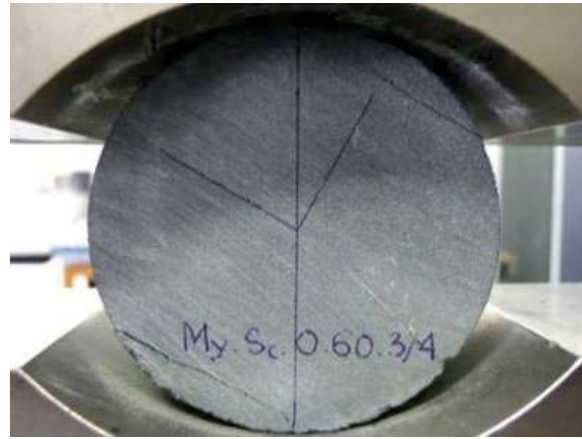
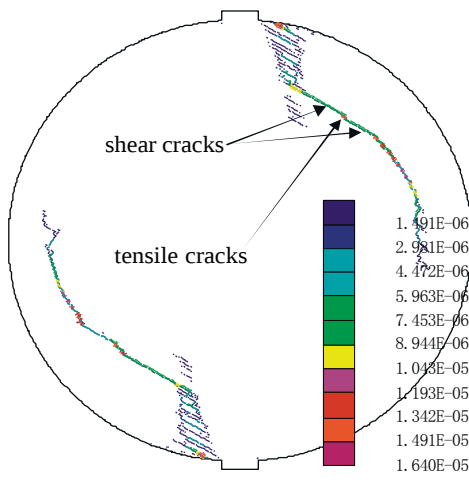


Micro-structural model of gneiss disc

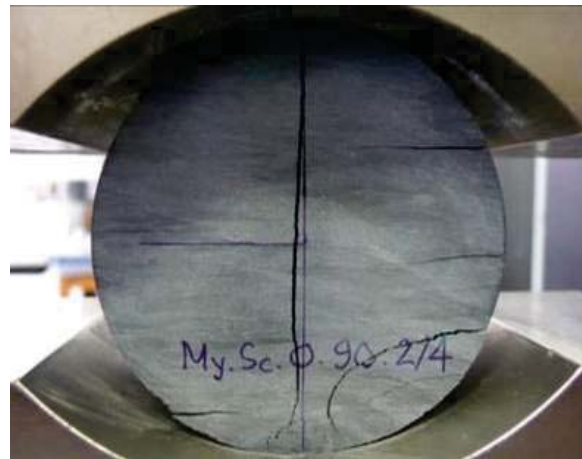
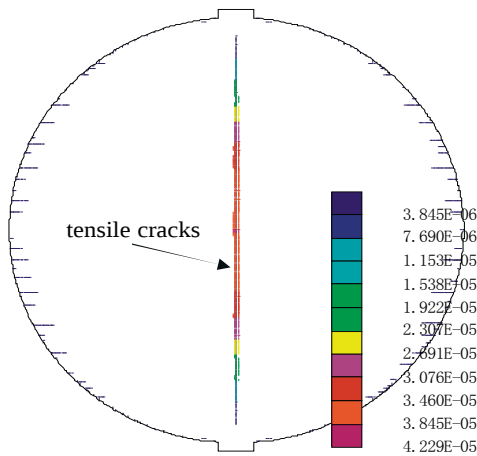


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Schist

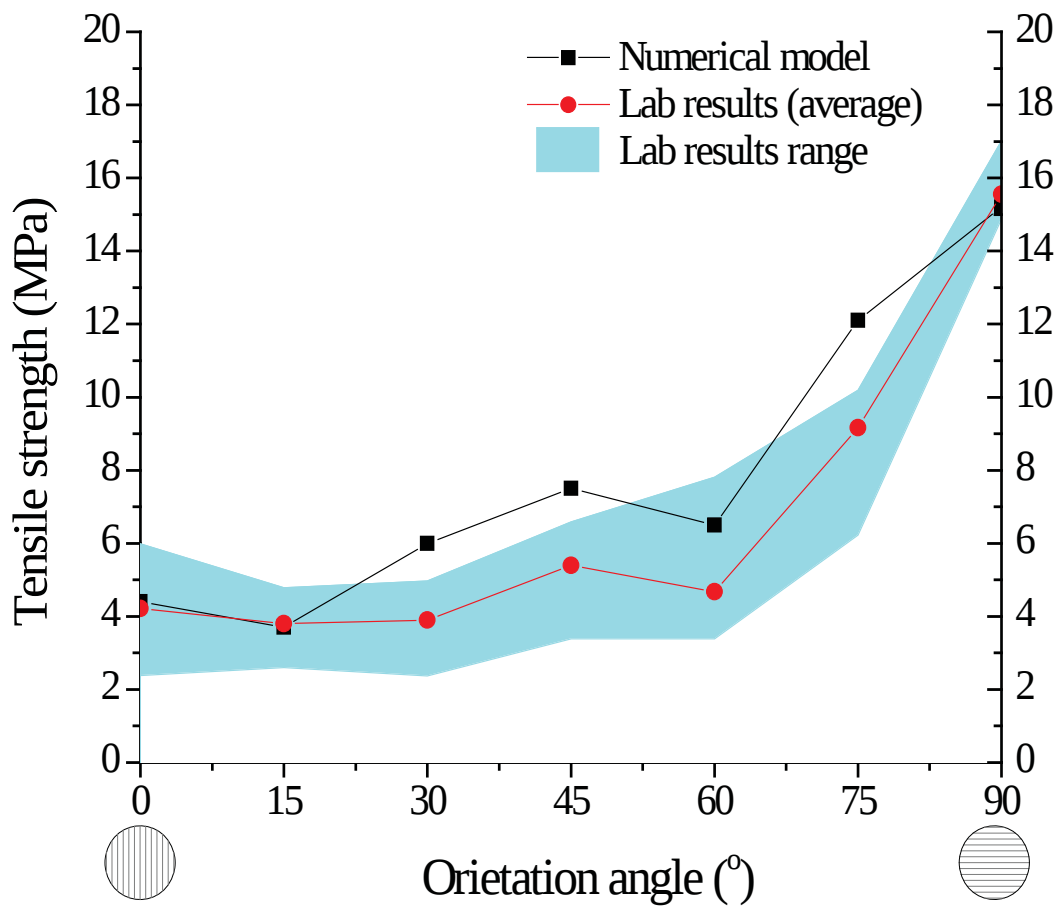


60°



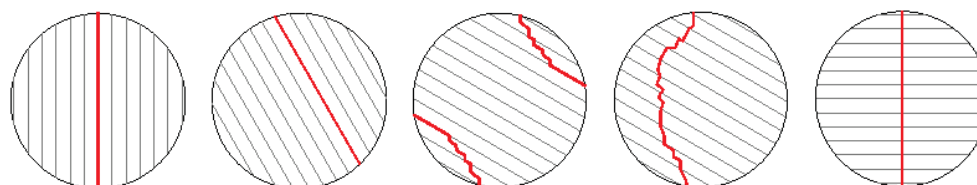
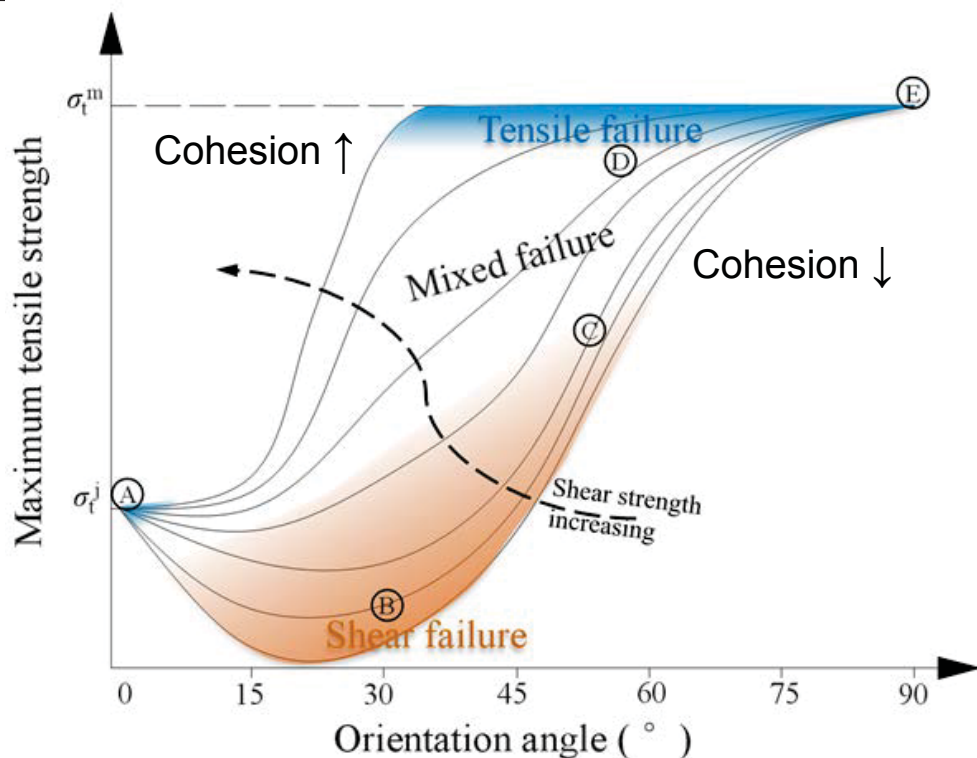
90°

17



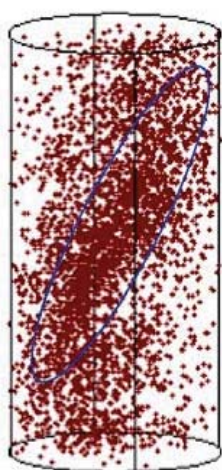
Schist

18



19

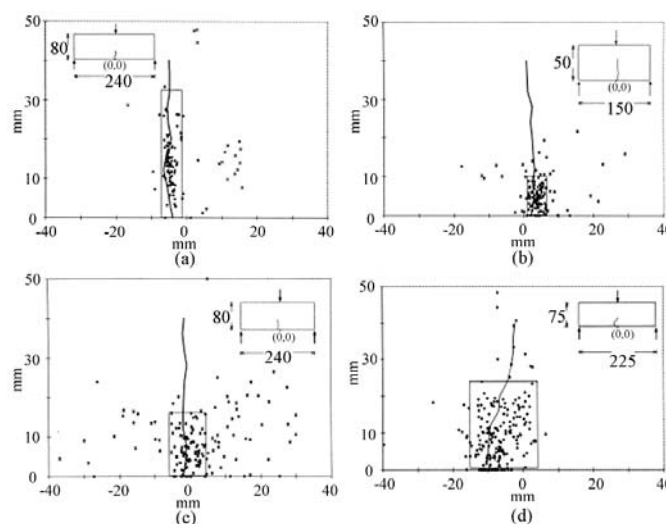
Lab test results



Spatial AE locations



Laboratory test



Spatial acoustic emission (AE) locations and experimental failure of red sandstone at a confining pressure of 35 MPa (Yang et al. 2012)

Acoustic emission (AE) locations and final macroscopic fracture pattern in the three-point bending test (a) Berea sandstone; (b) Sioux quartzite; (c) Charcoal granite; (d) Rockville granite (Zietlow and Labuz 1998)

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Theories and approaches utilized

Linear elastic fracture mechanics

Stress intensity factor approach

Subcritical crack growth theory

Charles equation

Crack propagation schemes

Elasto-plastic stress redistribution

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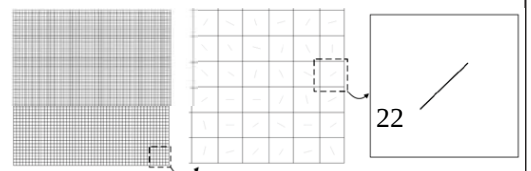
Subcritical crack growth simulation
using Charles equation and cellular
automate

$$t_{zone} = \int_{c_0}^{c_c} \frac{dc}{v}$$

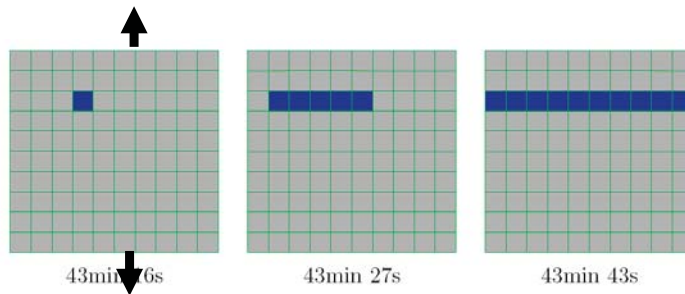
$$c_c = \min \{c_{Ic}, c_{IIc}, d_{zone}\} = \min \left\{ \frac{2}{\pi} \left(\frac{K_{Ic}}{\sigma} \right)^2, \frac{2}{\pi} \left(\frac{K_{IIc}}{\tau} \right)^2, d_{zone} \right\}$$

$$t_{zone} = \int_{c_0}^{c_c} [v(K_I) + v(K_{II})]^{-1} dc = \int_{c_0}^{c_c} [AK_I^n + AK_{II}^n]^{-1} dc$$

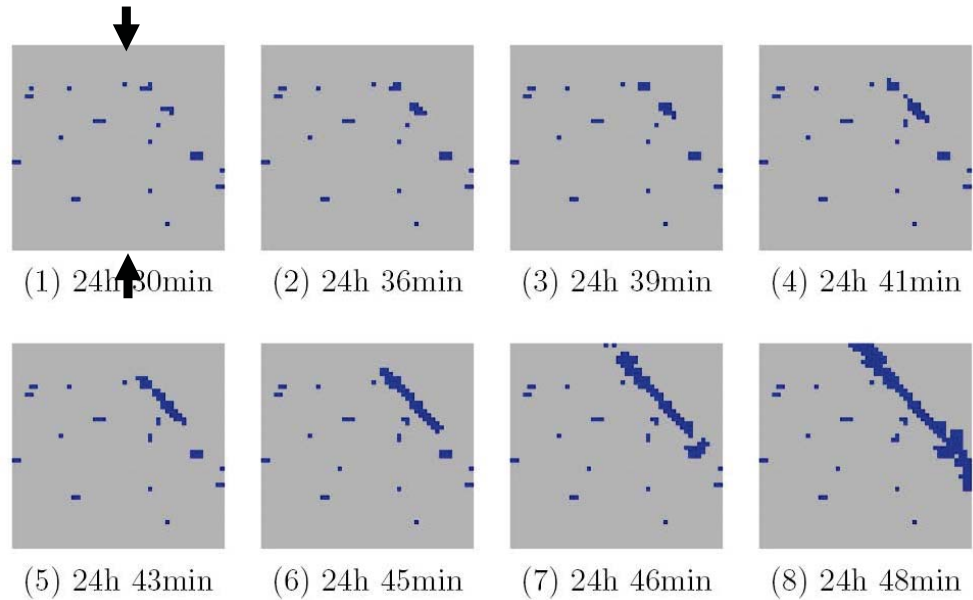
$$\begin{aligned} t_{zone} &= \frac{1}{A} \int_{c_0}^{c_c} \left[\left(\sigma \left(\frac{1}{2} \pi c \right)^{1/2} \right)^n + \left(\tau \left(\frac{1}{2} \pi c \right)^{1/2} \right)^n \right]^{-1} dc \\ &= \frac{1}{A(\sigma^n + \tau^n)} \left(\frac{2}{\pi} \right)^{n/2} \int_{c_0}^{c_c} c^{-n/2} dc \\ &= \frac{1}{A(\sigma^n + \tau^n)} \left(\frac{2}{\pi} \right)^{n/2} \frac{c_c^{1-n/2} - c_0^{1-n/2}}{1 - n/2} \end{aligned}$$



uniaxial
tension



uniaxial
compression

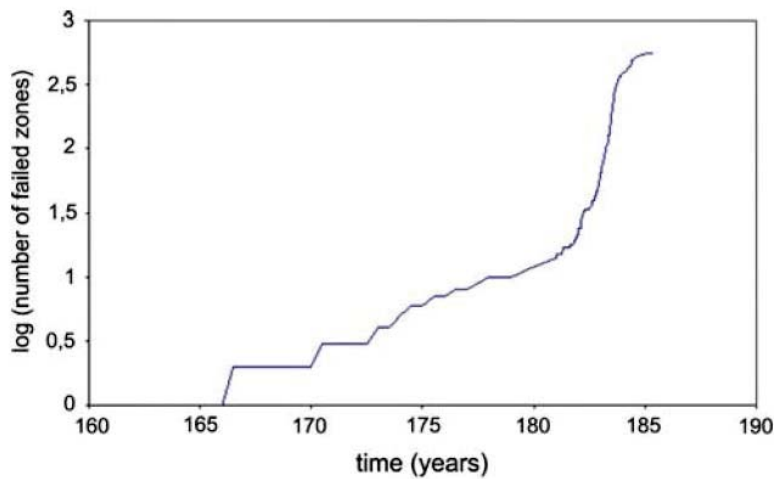


Typical damage development during uniaxial loading

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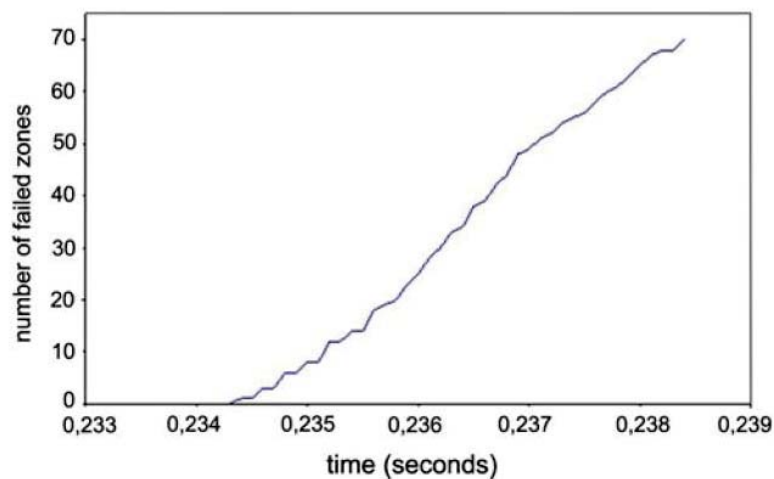
Konietzky, Heftenberger & Feige 2009

Comparison: damage development
under uniaxial compression and tension



Compressive load

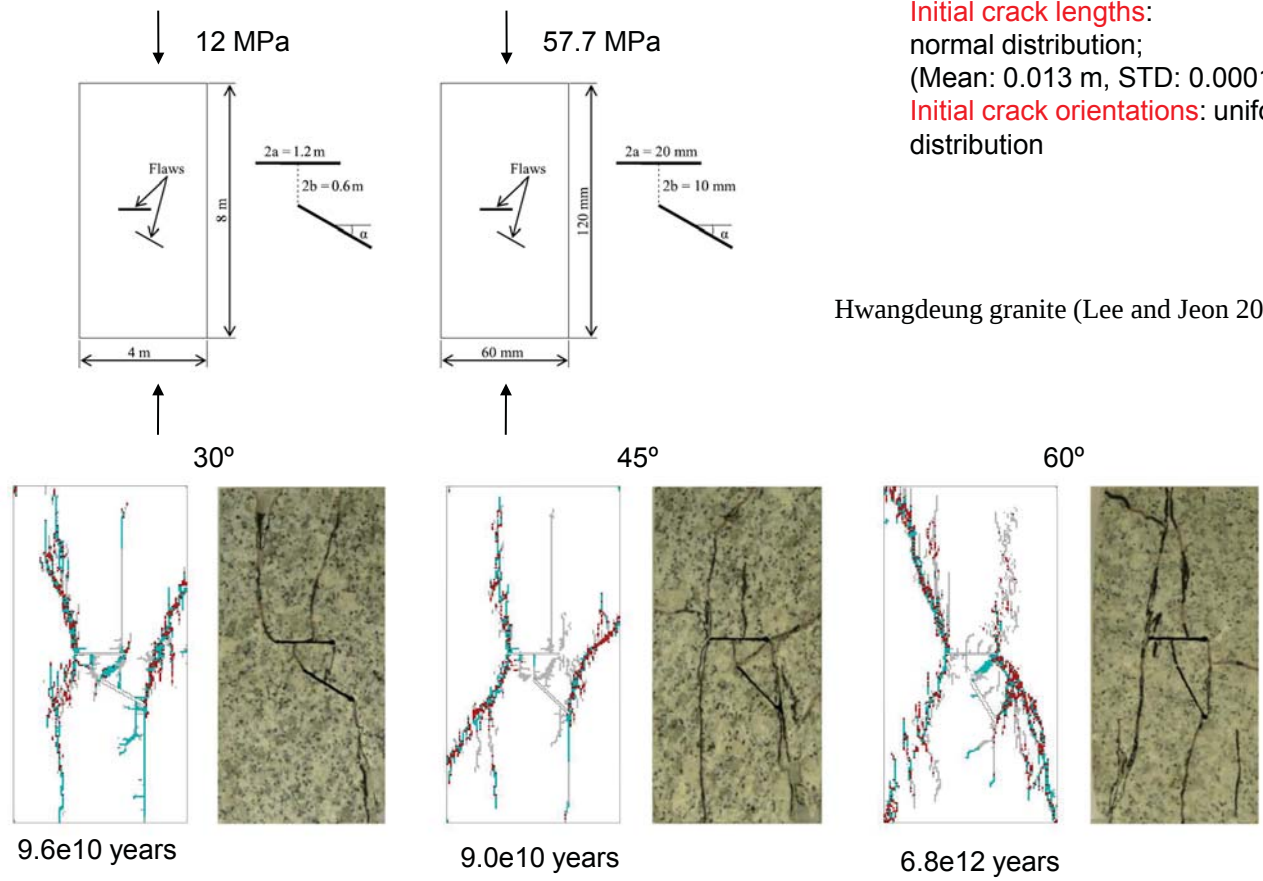
**Same load
magnitude !!**



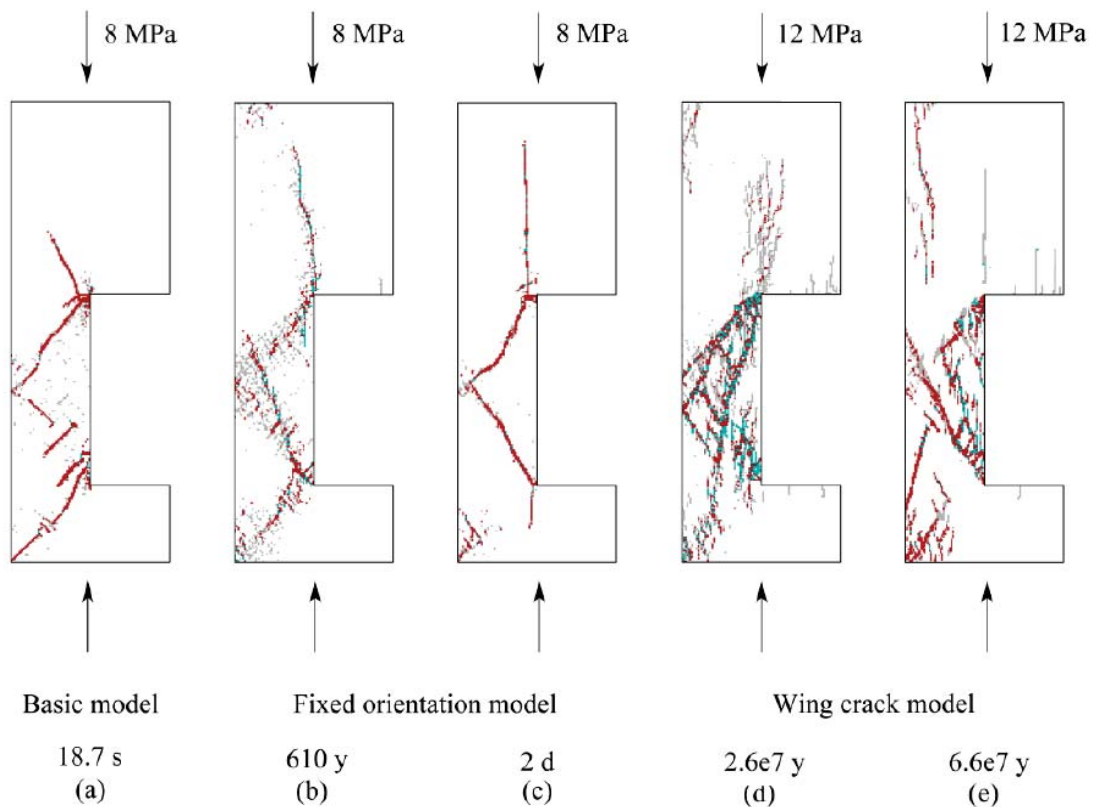
Tensile load

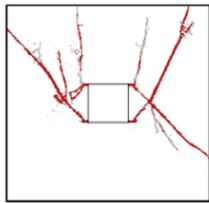
24

Zone size: 0.04 m;
Initial crack lengths:
normal distribution;
(Mean: 0.013 m, STD: 0.0001 m)
Initial crack orientations: uniform
distribution

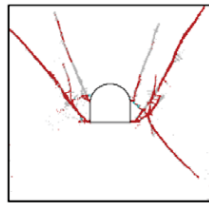


Practical Application: Pillar

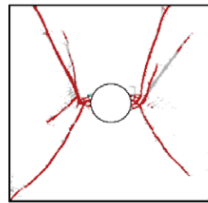




3 y
(a)



33 y
(b)

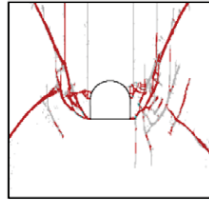


78 y
(c)

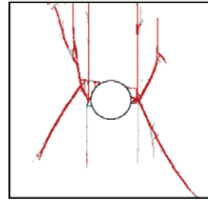
Basic model



2.5e6 y
(d)

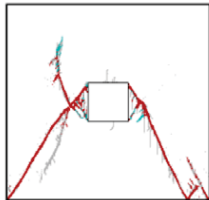


3.7e6 y
(e)

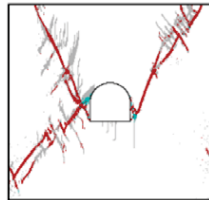


1.4e7 y
(f)

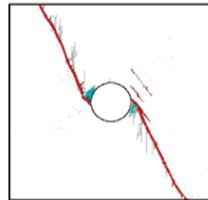
Fixed orientation model



3.3e18 y
(g)



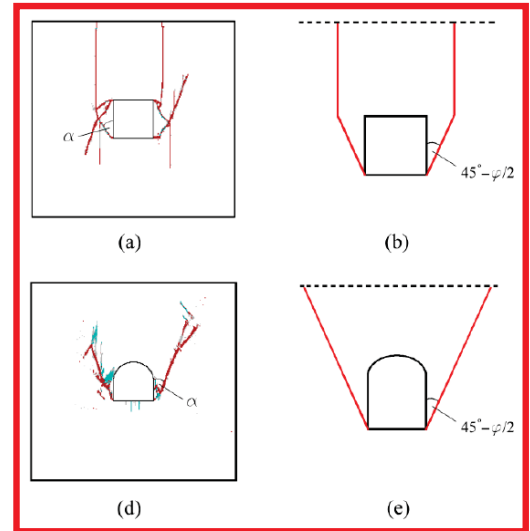
3.1e19 y
(h)



3.2e21 y
(i)

Wing crack model

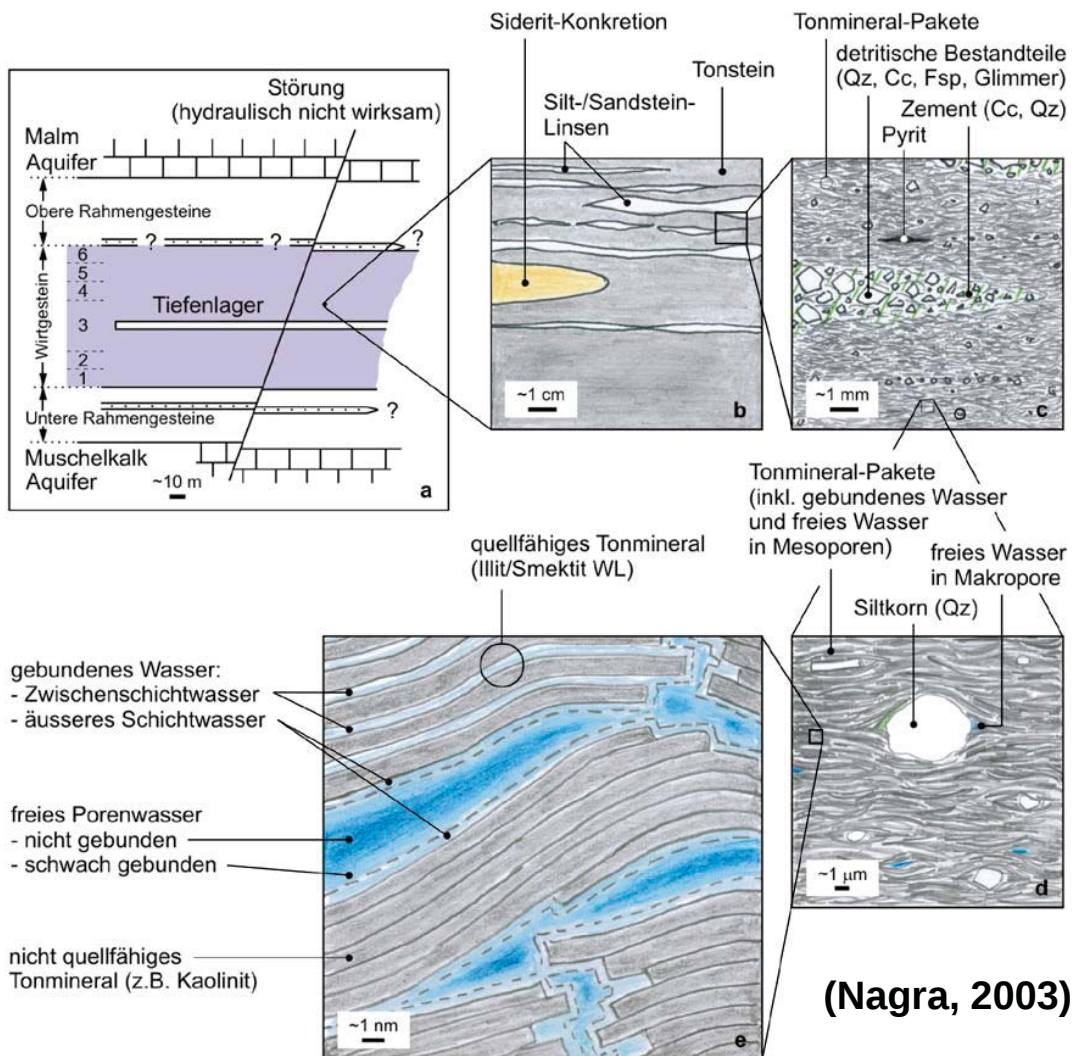
Practical Application: Tunnel , Drift



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Li & Konietzky 2013

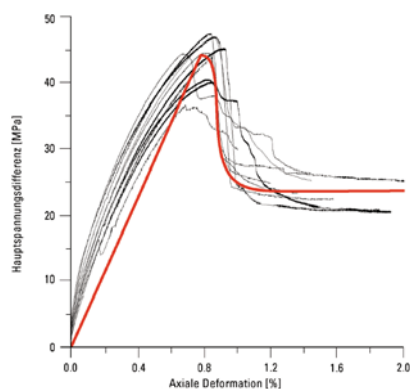
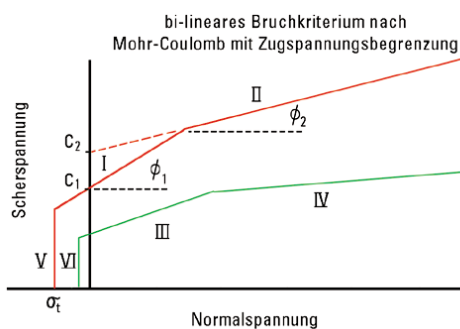
Model concepts for Opalinus clay



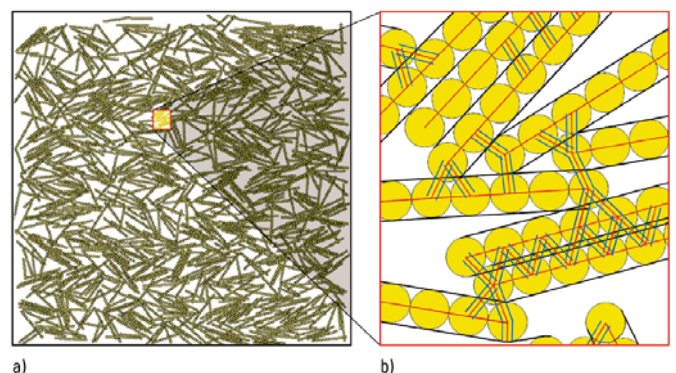
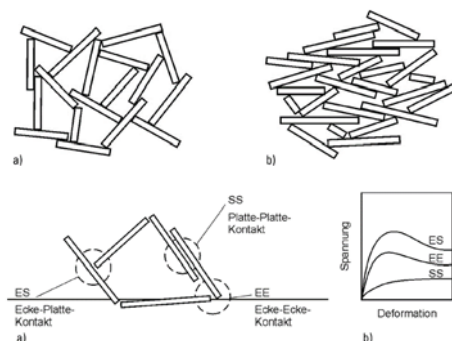
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2 concepts

„Phenomenological“ concept



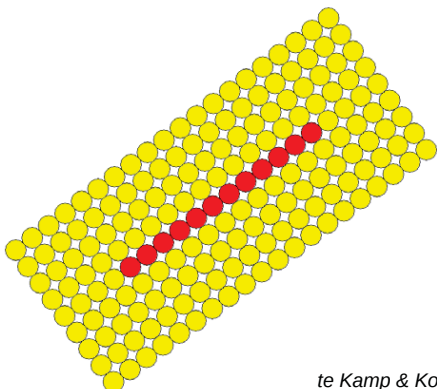
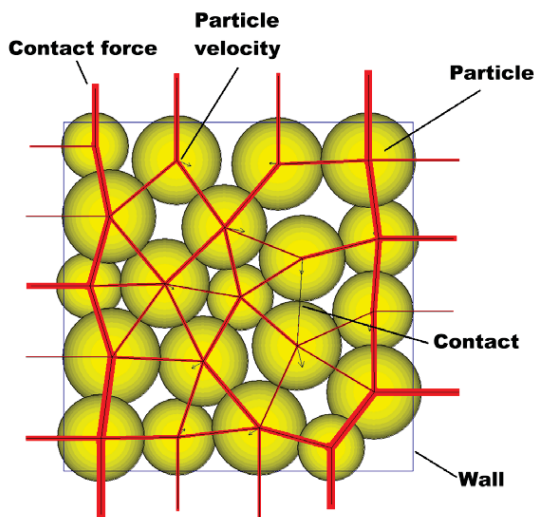
„Physical“ concept



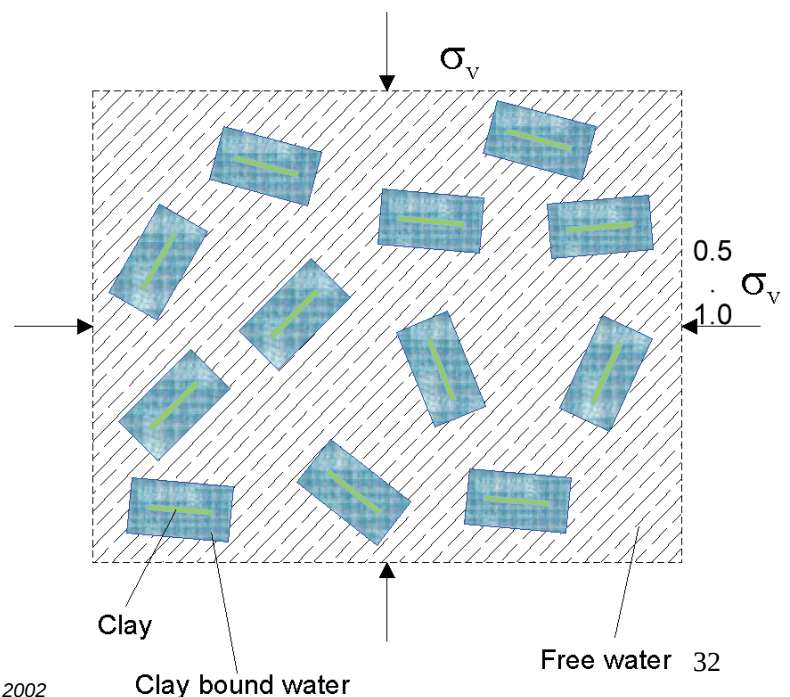
„Physical“ concept at the micro-scale

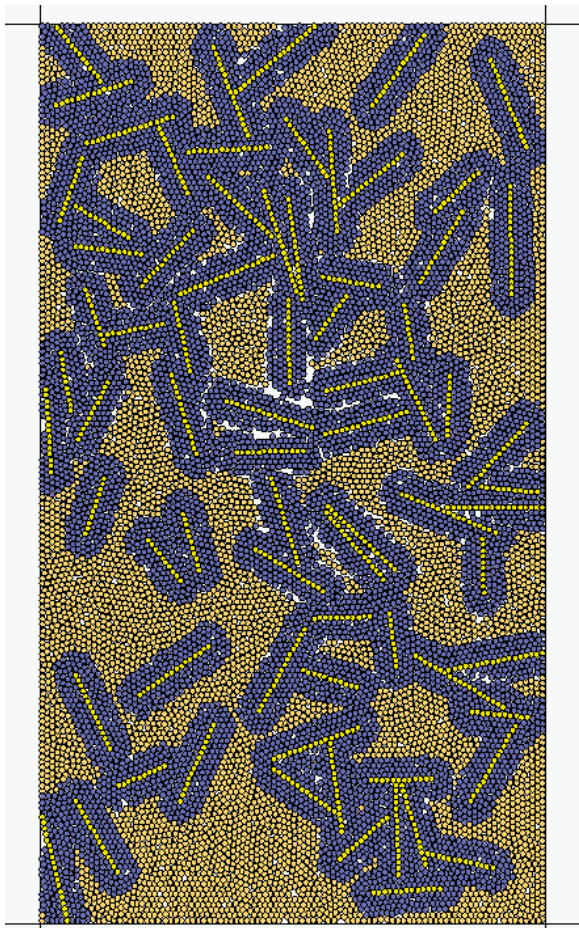


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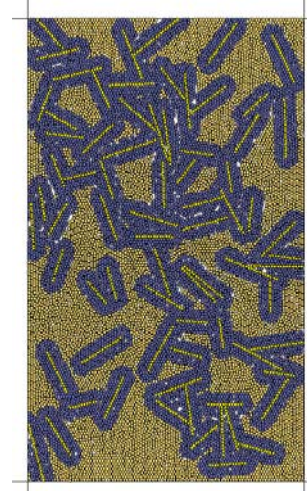
Numerical model
with clay plates, free water and
bounded water
(Lennard-Jones-Potential)



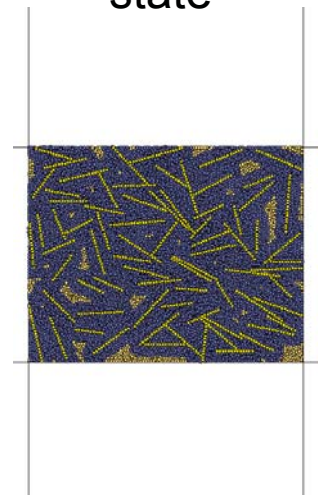


Model set-up

Initial
state



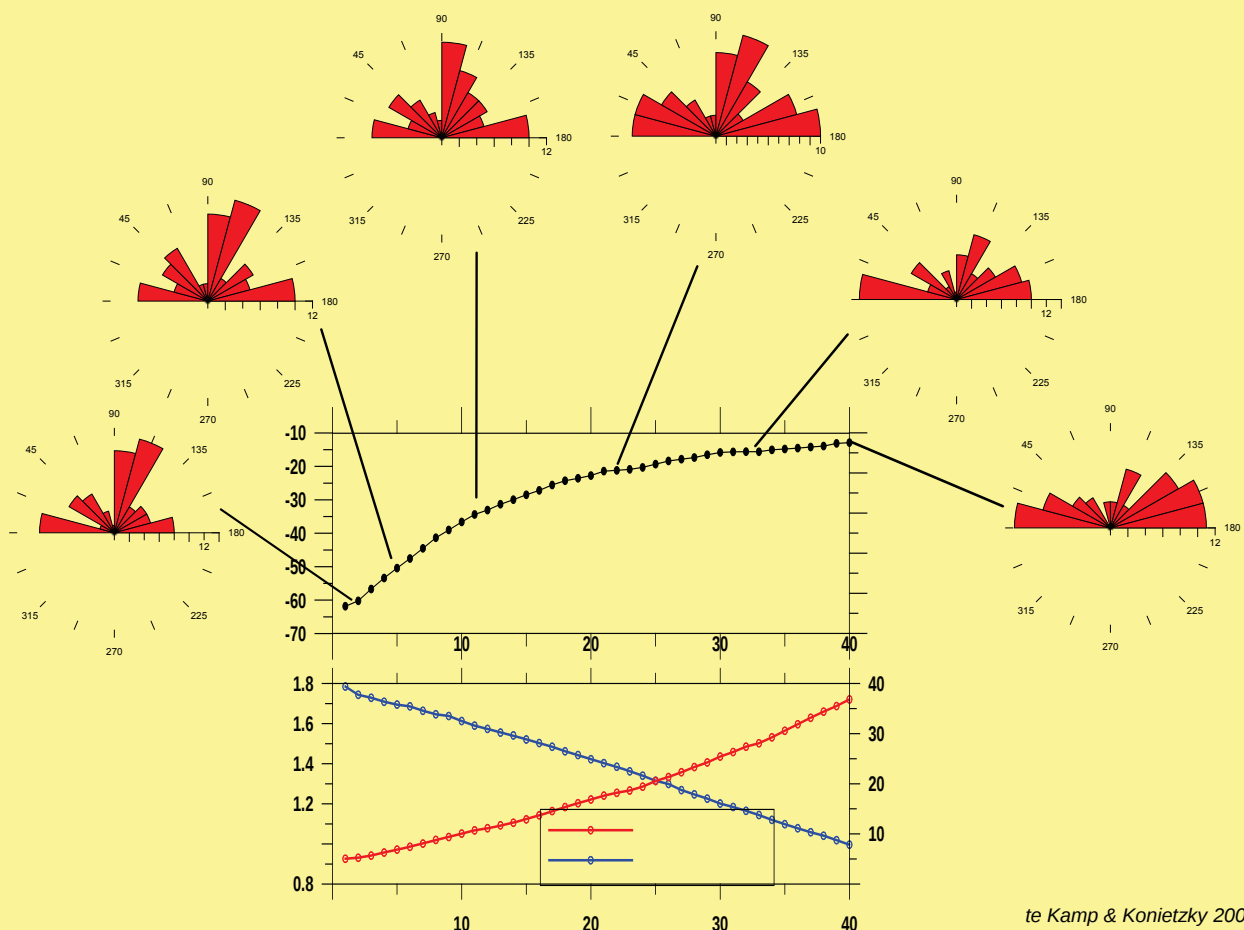
Final
state



Compaction of
saturated clay package
under loading

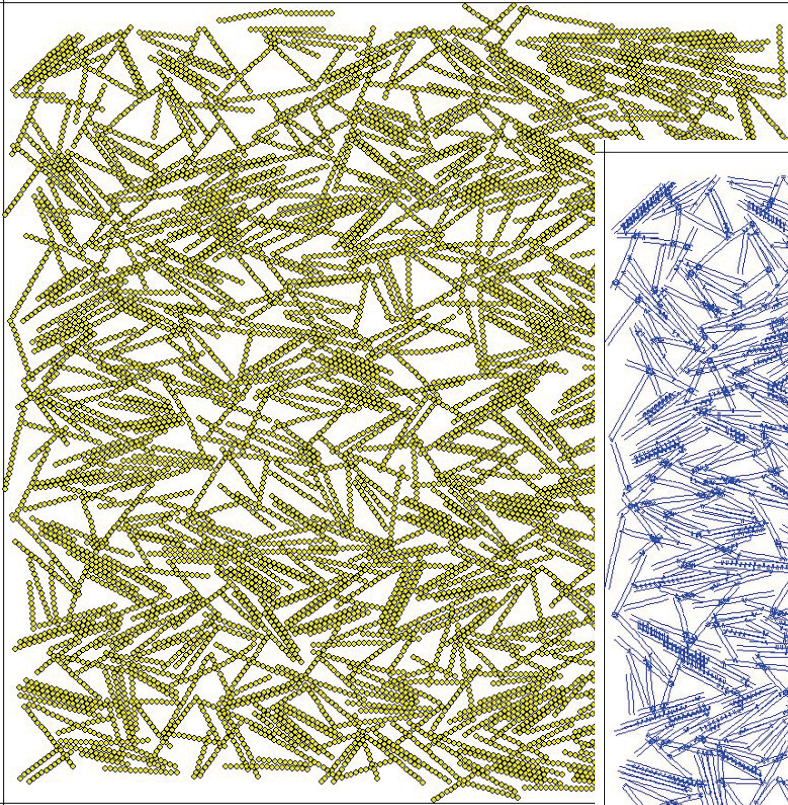
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Re-orientation of clay plates during compaction process

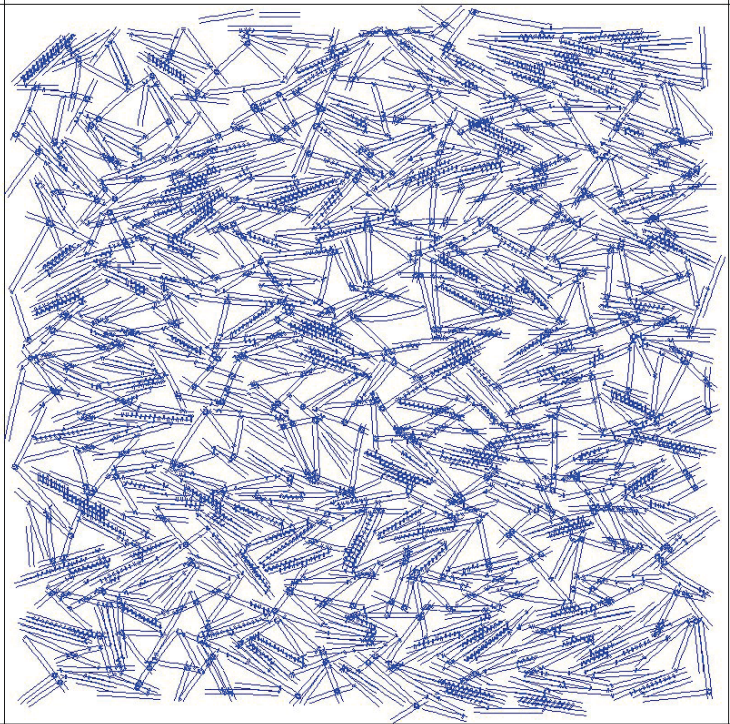


te Kamp & Konietzky 2002

Clay plate model without explicit consideration of water

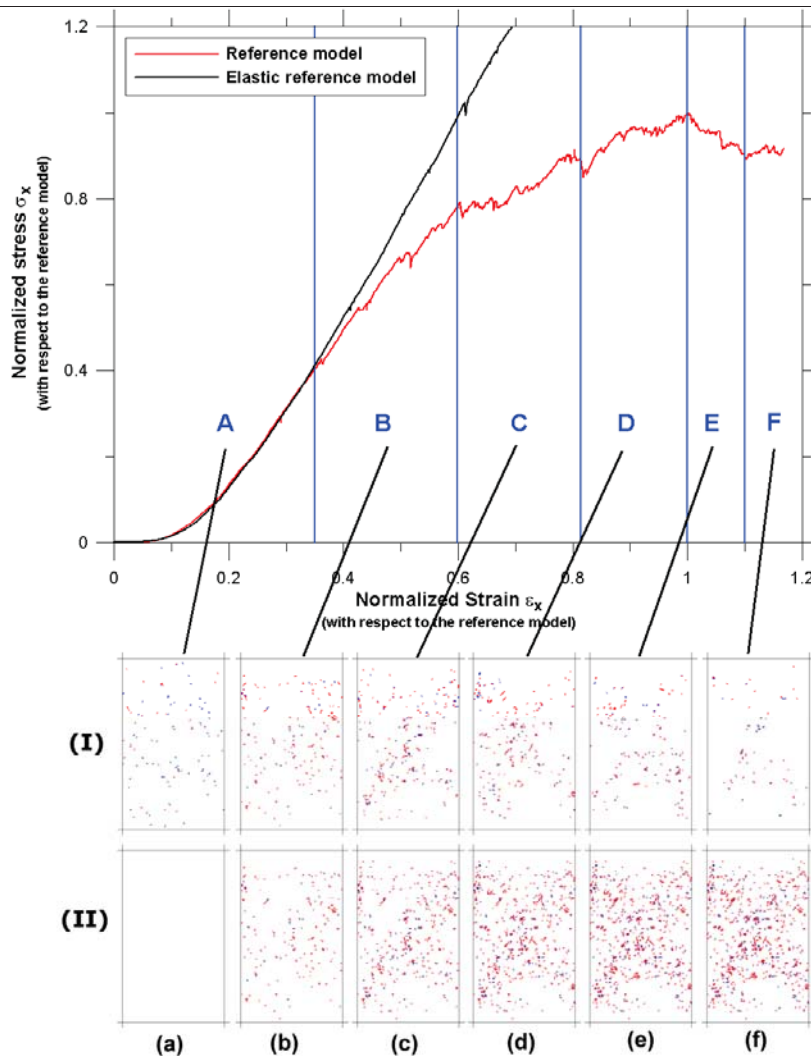


Porosity
app. 50%



te Kamp & Konietzky 2002

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Stress strain behaviour
and fracture pattern
of numerical
clay stone model

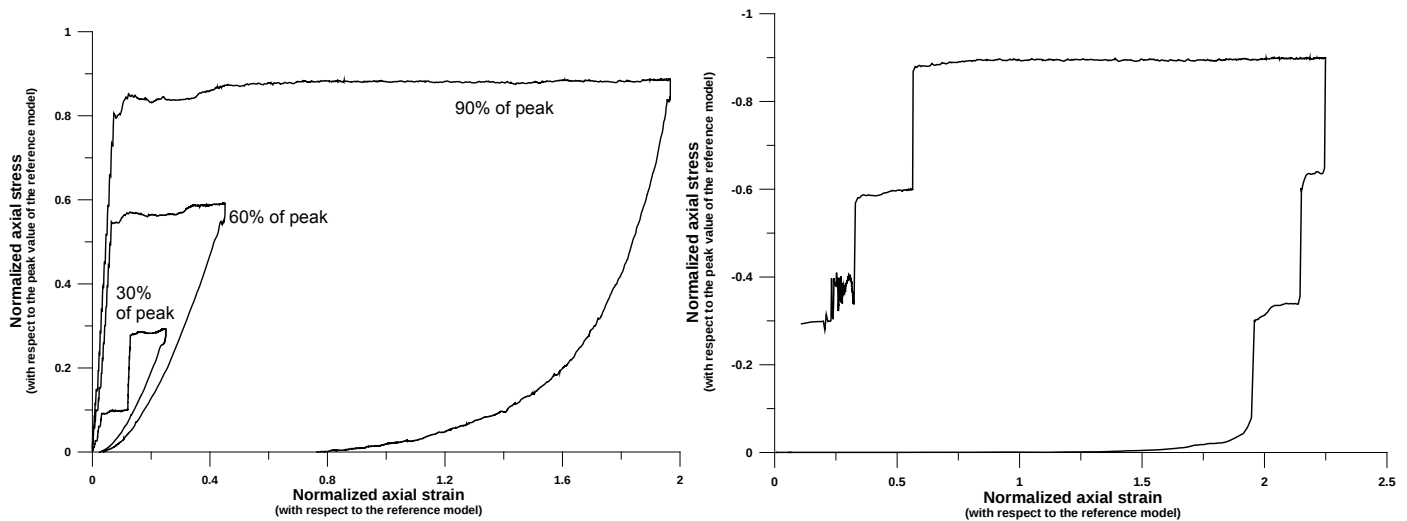
I: accumulated cracks

II: new cracks per phase

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te Kamp & Konietzky 2002

Compaction under constant load levels (note: irreversible plastic deformations)

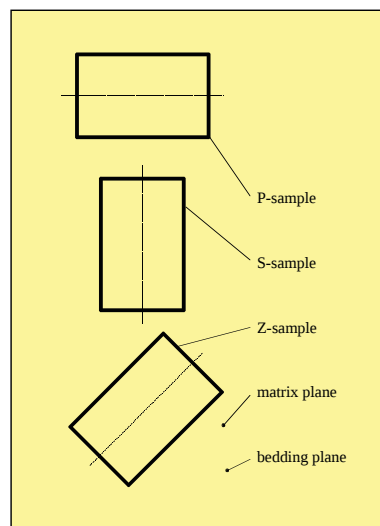
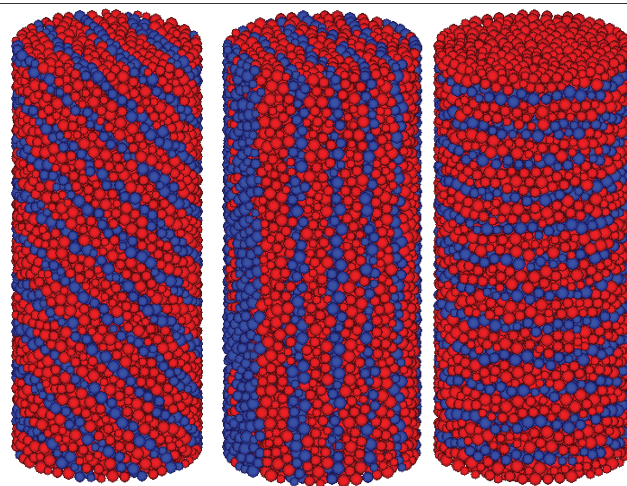
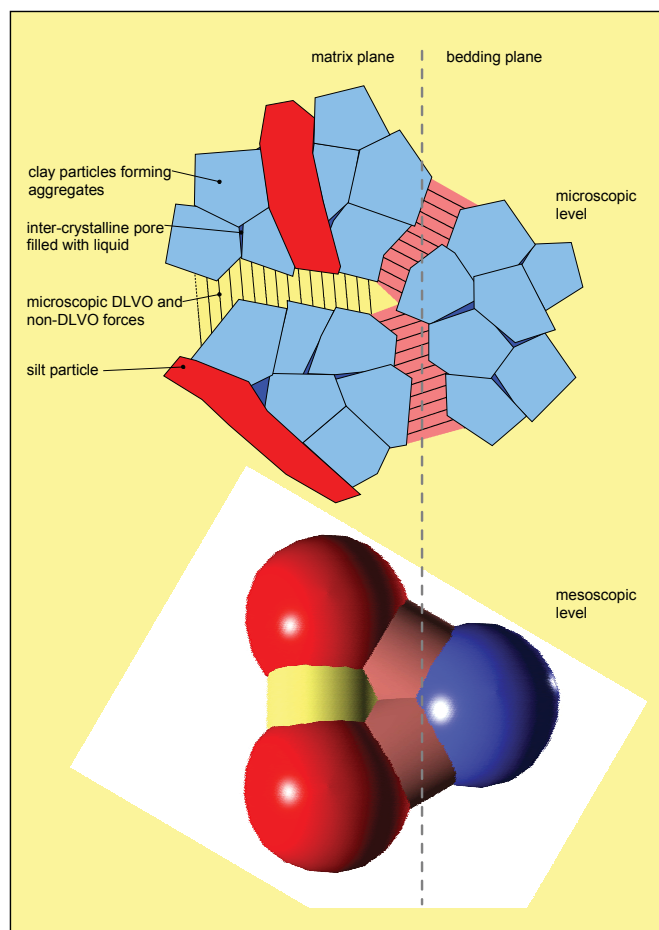


te Kamp & Konietzky 2002

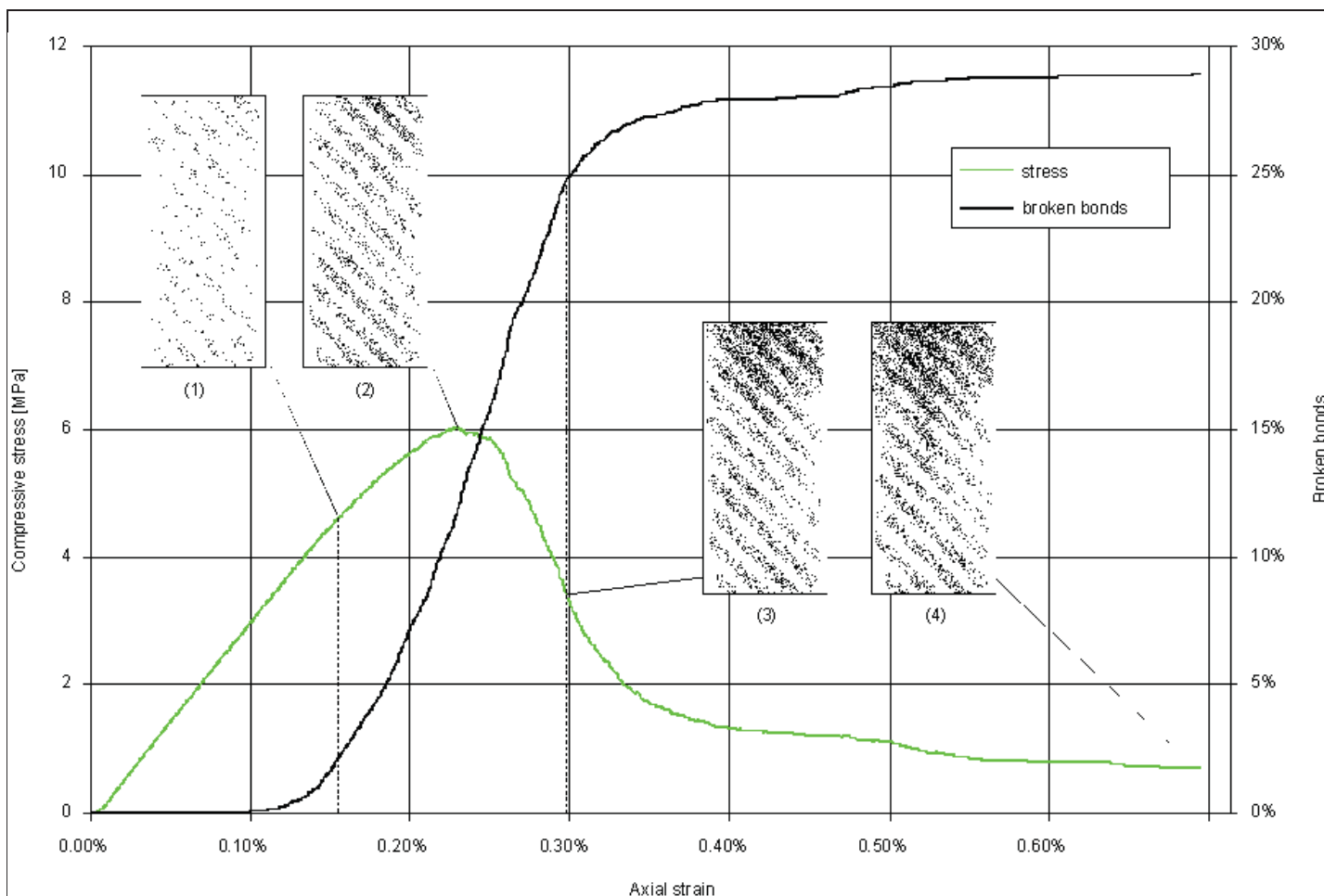
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„Physical“ concept at the meso-scale

Anisotropic model for Opalinus Clay



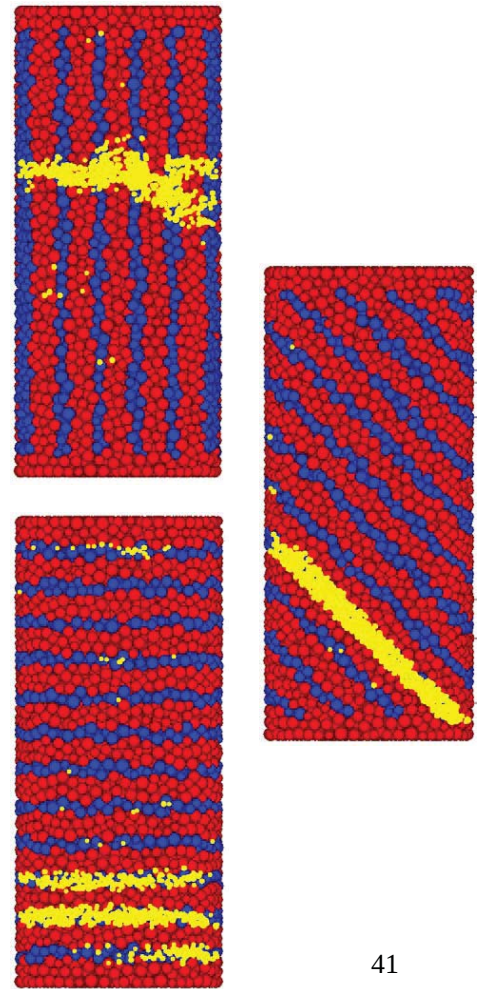
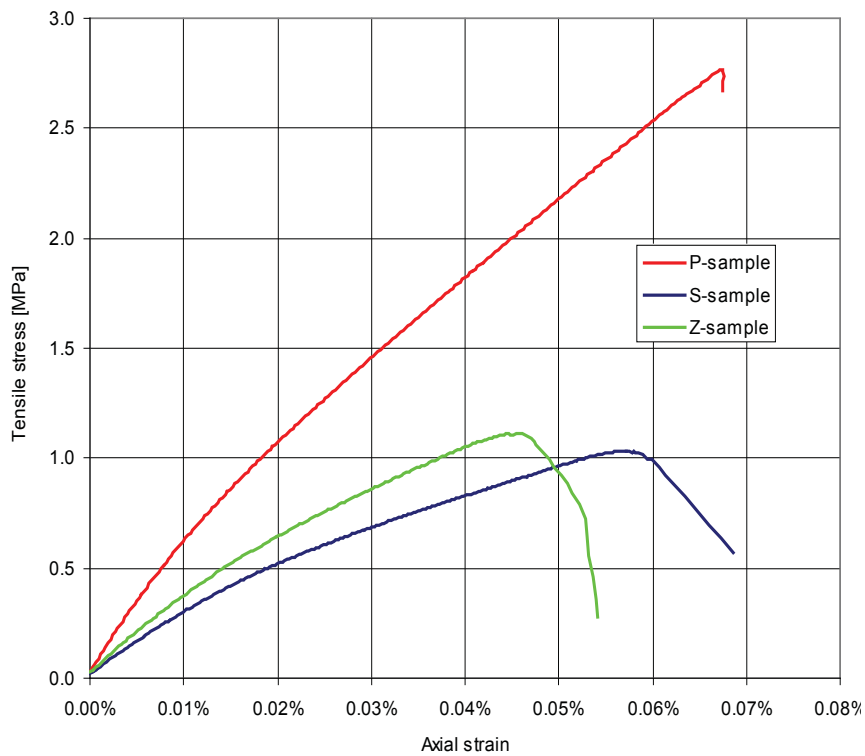
39



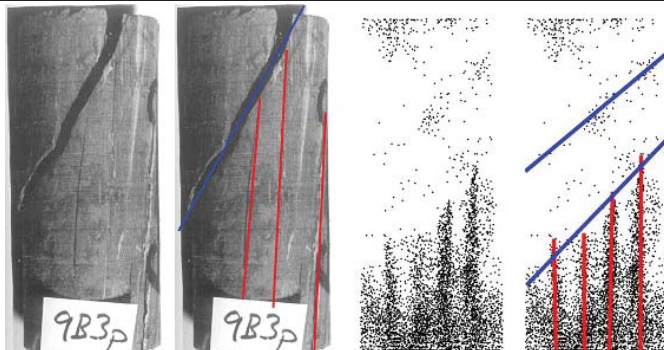
Stress – strain behaviour and fracture pattern: uniaxial compression test (S-Sample)

40

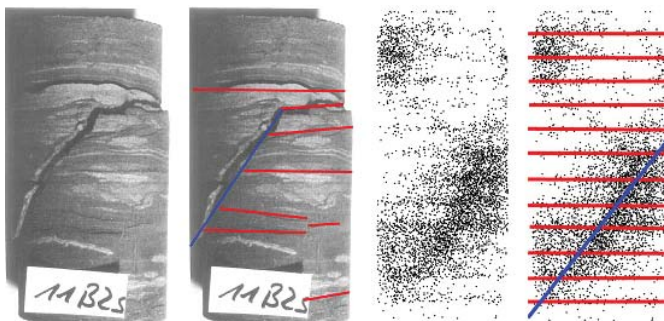
Uniaxial tensile testing: stress-strain curves and fracture pattern



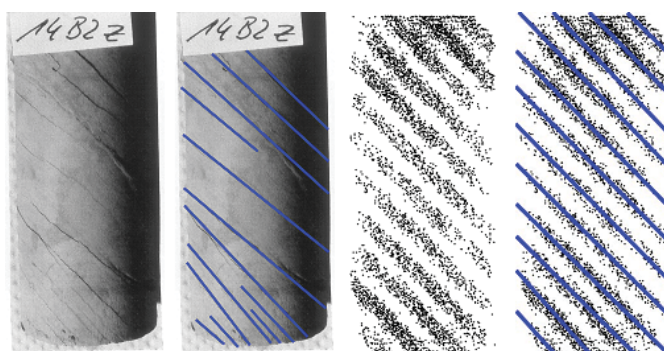
41



P-Sample



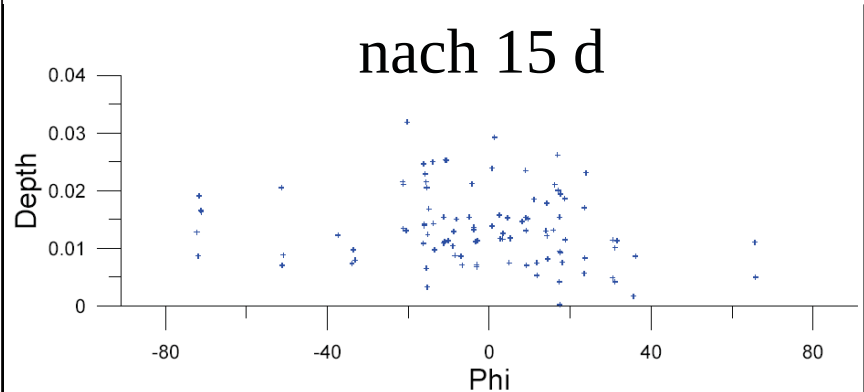
S-Sample



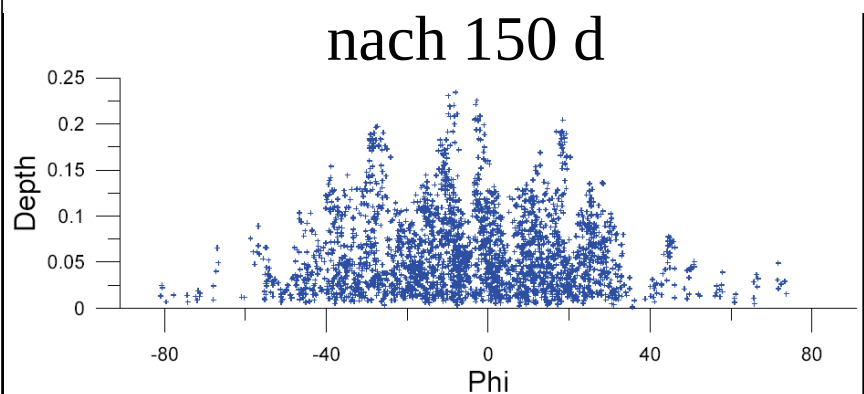
Z-Sample

Uniaxial
compression:
fracture pattern
lab vs. model

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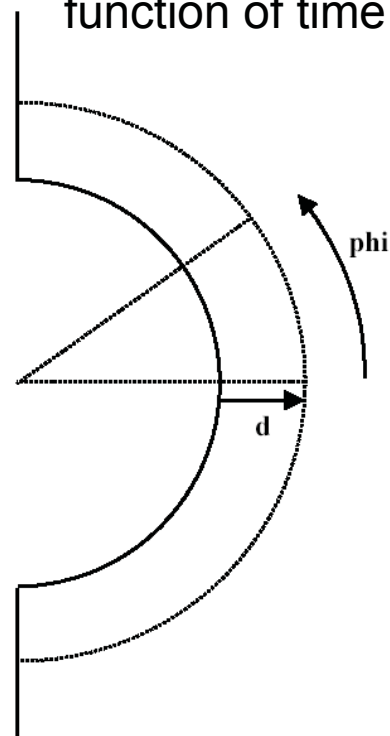


c) Développée du tunnel donnant les positions des micro-fractures (angle en °, profondeur en m)

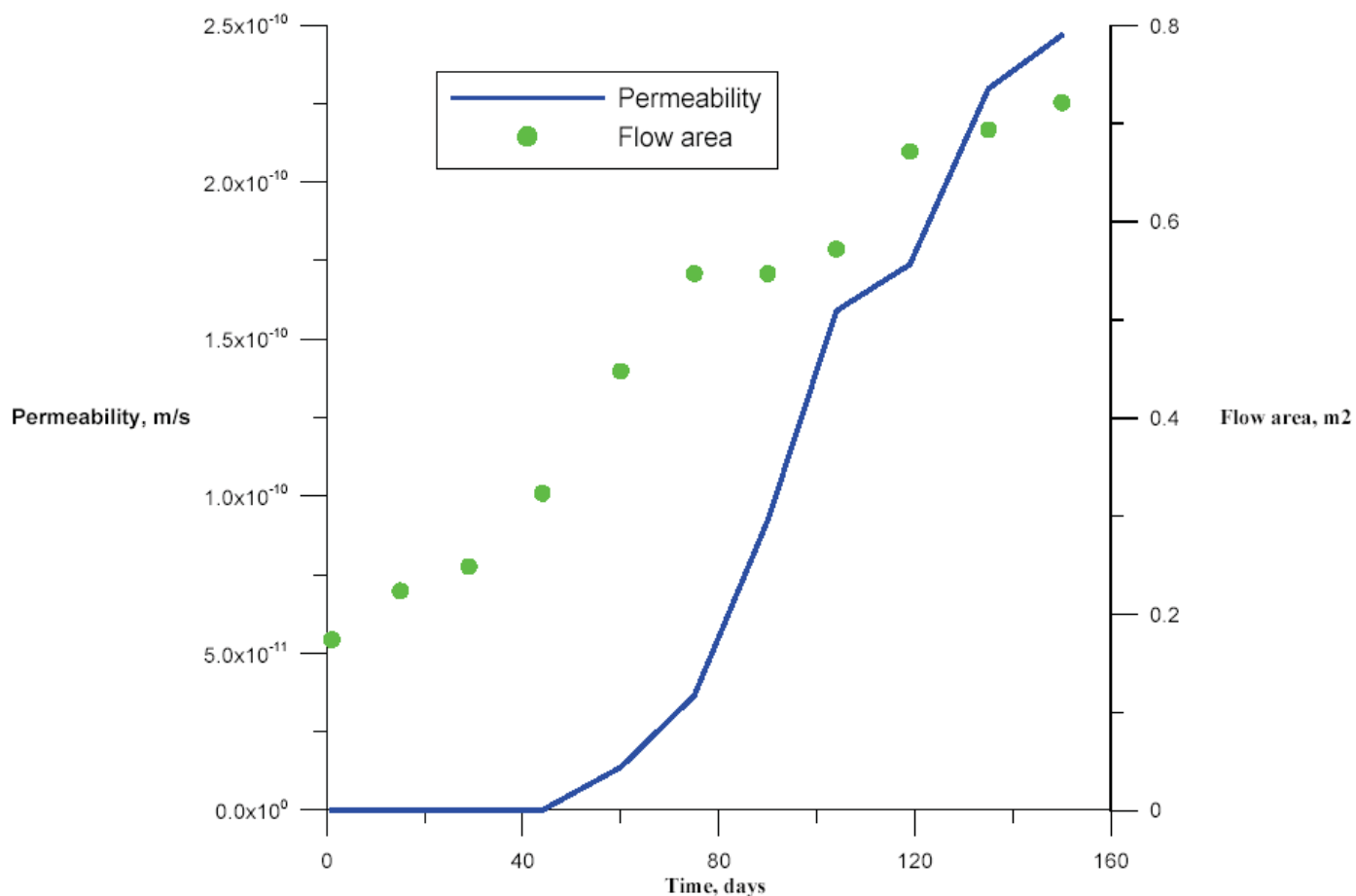


c) Développée du tunnel donnant les positions des micro-fractures (angle en °, profondeur en m)

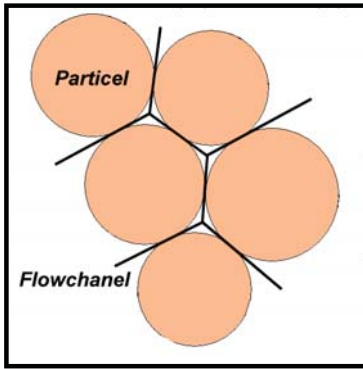
EDZ:
fracture pattern as
function of time



Permeability and flow area development in EDZ vs. time



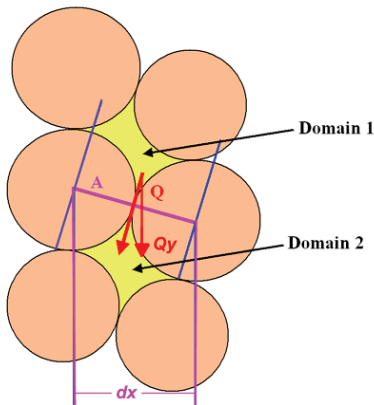
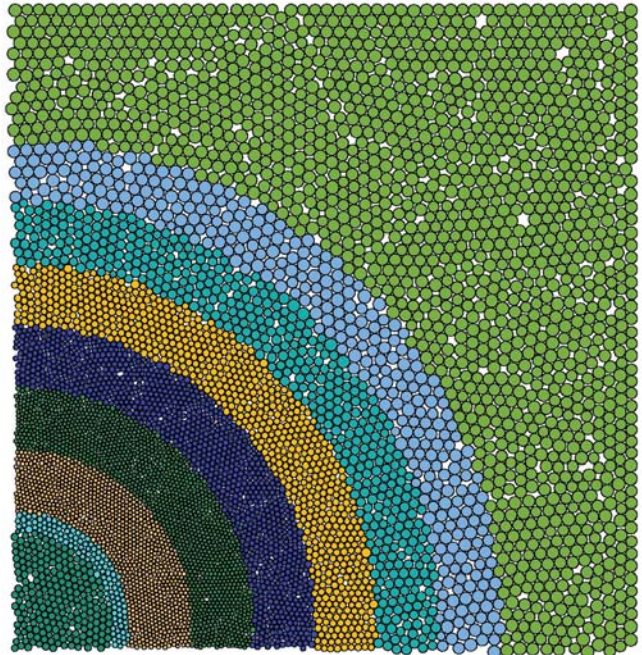
EDZ-study: Mt. Terri, tunnel radius = 1.8 m



$$\Delta P = -K \frac{\Delta V}{V}$$

$$\dot{Q} = Ka^3 \frac{\Delta P}{\Delta X}$$

$$a = \frac{a_0 F_0}{F + F_0}$$



Numerical model set-up and
Illustration of HM-coupling scheme

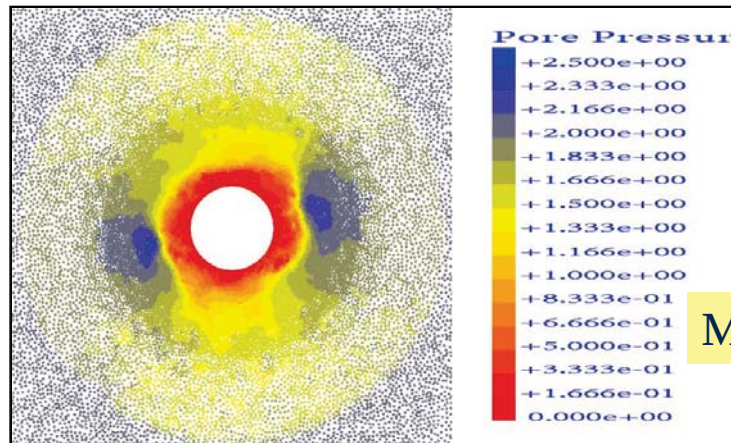
te Kamp, Konietzky & Blümling 1999
Konietzky, te Kamp & Blümling 2001

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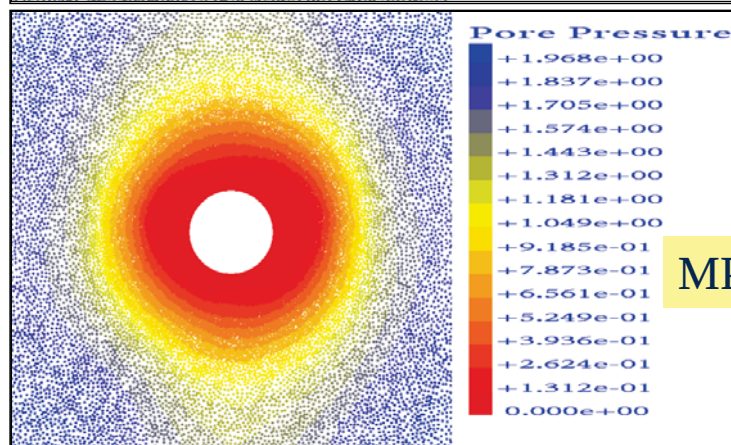
$P_{p,ini} = 2 \text{ MPa}$

1 day

1 month



MPa

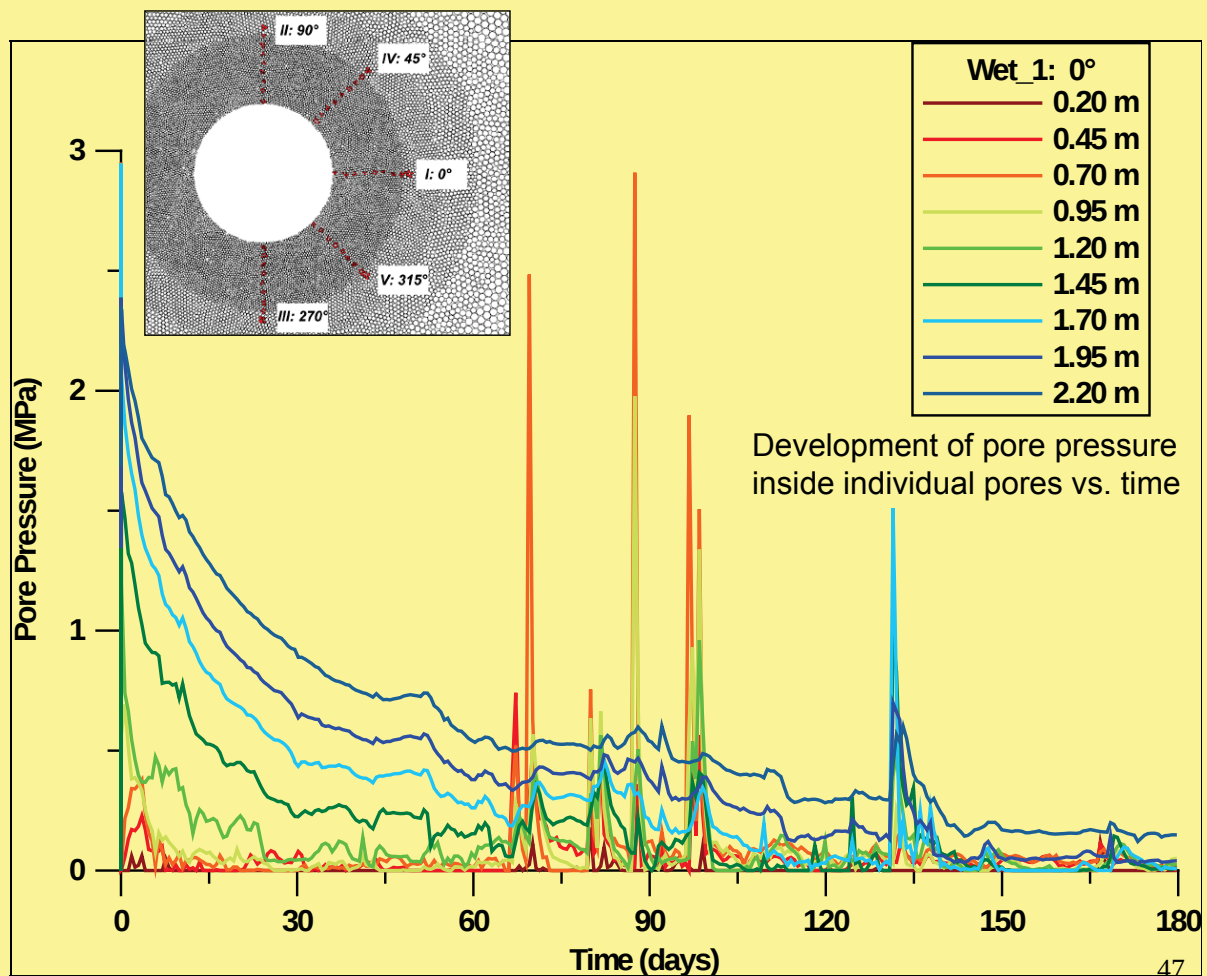


MPa

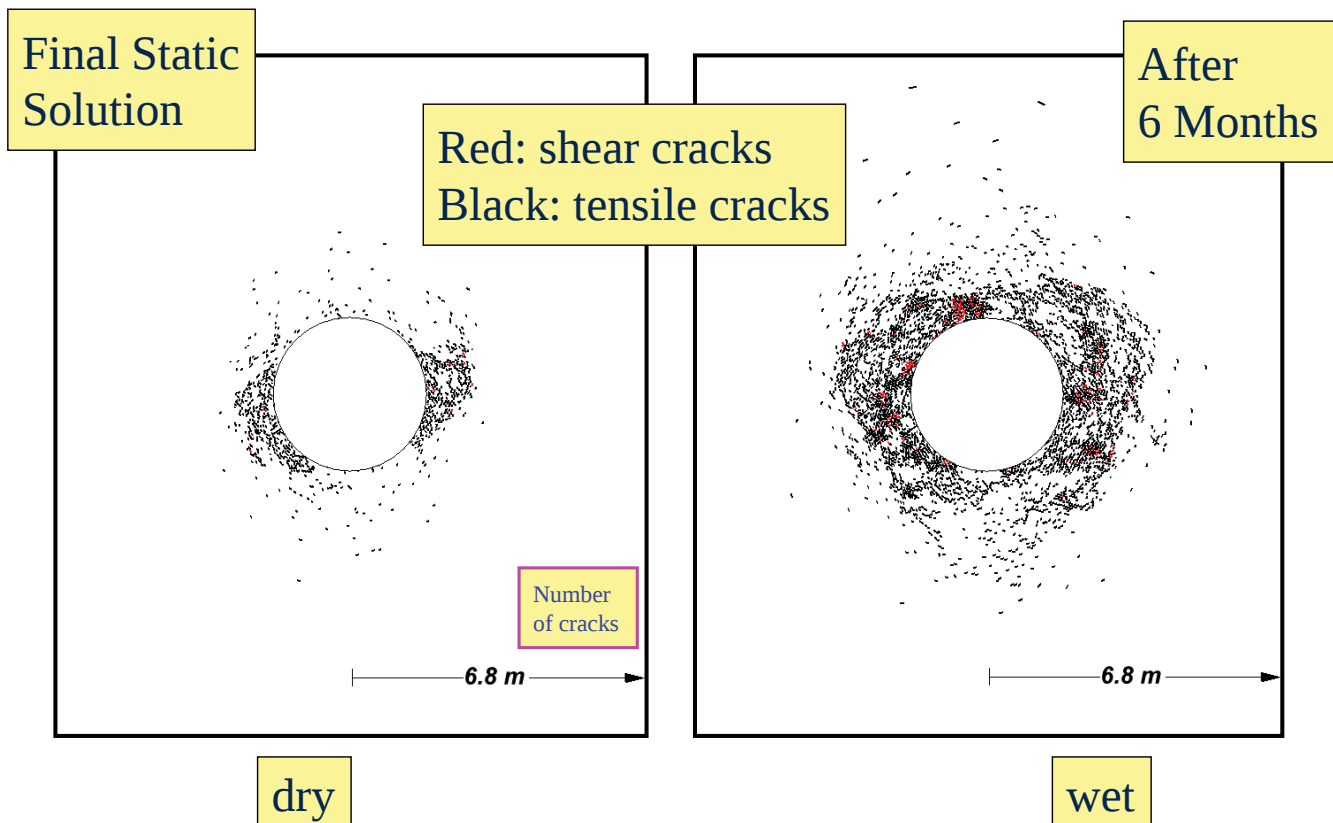
Pore pressure distribution around opening

te Kamp, Konietzky & Blümling 1999
Konietzky, te Kamp & Blümling 2001

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te Kamp, Konietzky & Blümling 1999
Konietzky, te Kamp & Blümling 2001

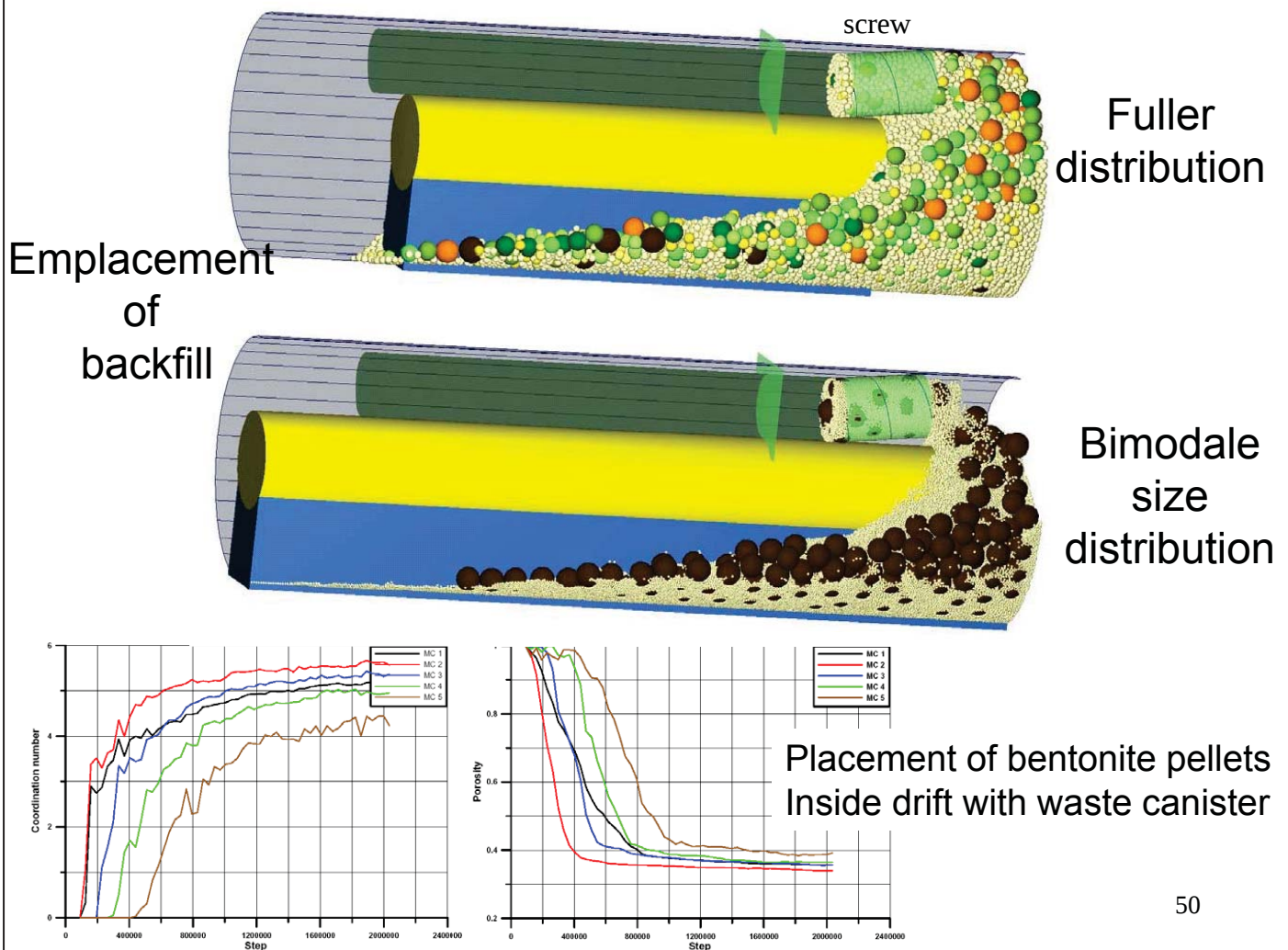


Comparison: damage state under dry and wet conditions

Simulation potential at the meso/macro-scale based on DEM technique



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Verständnis mikromech. Prozesse = Voraussetzung für fundierte Prognose

Knowledge micromech. Processes = Prerequisite for reliable Prediction

Correct micro- and meso-mechanical simulation demands the explicit consideration of:

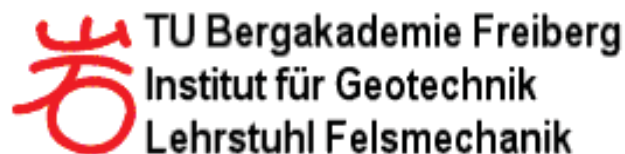
- Grain shapes
- Grain size distribution
- Initial damage
- Intragranular and intergranular fracturing
- Porosity (shape, size, distribution)
- Mineral components / phases
- Critical and subcritical crack growth
- Simulation of granular flow and compaction

Korrekte mikro- und meso-mechanische Simulationen erfordern die explizite Berücksichtigung von:

- Kornform
- Korngrößenverteilung
- Initiale Schädigung
- Intragranulare und intergranul. Bruchprozesse
- Porosität (Form, Größe, Verteilung)
- Mineralbestand
- Kritisches und subkritisches Risswachstum
- Simulation of Partikelströmen und Kompaktion

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Thanks for your kind attention



Following co-workers have contributed to the presented results:

Dr. Li, Dr. te Kamp, Dr. Gröger, Dr. Tan, Mr. Baumgarten, Dr. Herbst, Dr. Groh